

Spin-Density Matrix Elements for Vector-Meson Photoproduction at GlueX

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for the GlueX Collaboration

15th International Conference on Meson-Nucleon Physics
and the Structure of the Nucleon (MENU2019)

Carnegie Mellon University, Pittsburgh, PA
June 3rd, 2019



Outline

1 Introduction

2 Method

- Extended Maximum-Likelihood Fit
- Fit Evaluation

3 Results

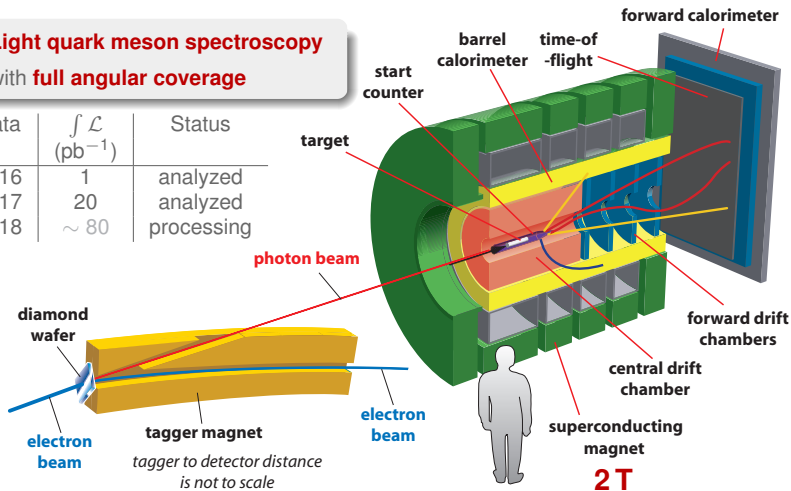
- $\rho(770) \rightarrow \pi^+ \pi^-$
- $\omega(782) \rightarrow \pi^+ \pi^- \pi^0$
- $\phi(1020) \rightarrow K^+ K^-$

4 Outlook

GlueX Detector

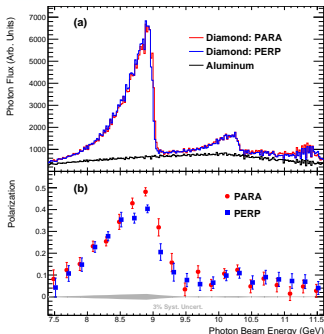
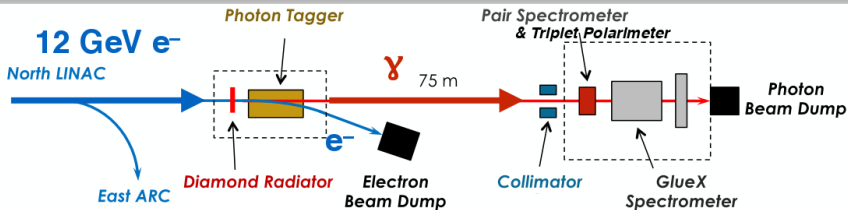
Light quark meson spectroscopy
with **full angular coverage**

Data	$\int \mathcal{L}$ (pb^{-1})	Status
2016	1	analyzed
2017	20	analyzed
2018	~ 80	processing



→ S. Dobbs, Searching for Exotic Hadrons at GlueX (Monday morning)

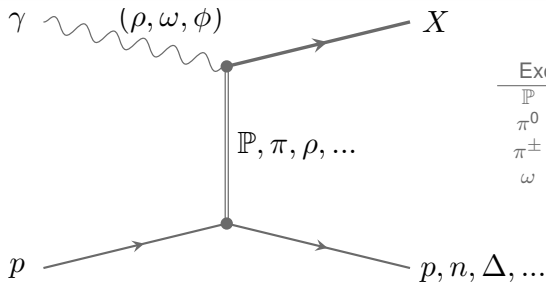
Photon Beam Line



9 GeV Polarized Photon Beam

- Coherent Bremsstrahlung on thin diamond
- Energy tagged by scattered electrons
- Collimator to suppress incoherent part
- Linear polarization in peak $P_\gamma \sim 40\%$, measured by Triplet polarimeter:
 $\gamma e^- \rightarrow e^- e^+ e^-$
- Rotate polarization into 4 different orientations
- Beam intensity: $1 - 5 \cdot 10^7 \gamma/s$ in peak

Photoproduction



Exchange		Exotic Final States	
\mathbb{P}	0^{++}	b, h, h'	$2^{+-}, 0^{+-}$
π^0	0^{-+}	b_2, h_2, h'_2	2^{+-}
π^\pm	0^{-+}	π_1^\pm	1^{-+}
ω	1^{--}	π_1, η_1, η'_1	1^{-+}

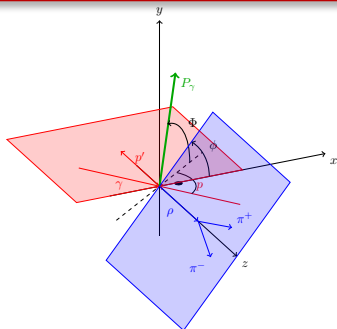
Complementary Production Mechanism

- Photon coupling via **vector meson dominance**
- Wide variety of quantum numbers $I^G J^{PC}$ accessible
- Photon polarization provides **constraints** on produced systems
- Understanding of **production mechanism** is prerequisite for interpretation
- Very limited photoproduction data existing at these energies

Production Mechanism

Spin-Density Matrix Elements

- Full angular distribution of vector meson production and decay is described by **spin-density matrix elements** ρ_{ij}^k
- Linear beam polarization provides access to **nine** linearly independent SDMEs
- Intensity W is expressed as function of angles **cos ϑ , φ , Φ** and degree of polarization **P_γ**



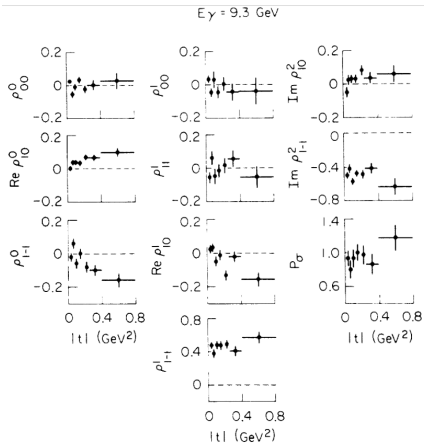
$$W(\cos \vartheta, \varphi, \Phi) = W^0(\cos \vartheta, \varphi) - P_\gamma \cos(2\Phi)W^1(\cos \vartheta, \varphi) - P_\gamma \sin(2\Phi)W^2(\cos \vartheta, \varphi)$$

$$W^0(\cos \vartheta, \varphi) = \frac{3}{4\pi} \left(\frac{1}{2}(1 - \rho_{00}^0) + \frac{1}{2}(3\rho_{00}^0 - 1) \cos^2 \vartheta - \sqrt{2}\text{Re}\rho_{10}^0 \sin 2\vartheta \cos \varphi - \rho_{1-1}^0 \sin^2 \vartheta \cos 2\varphi \right)$$

$$W^1(\cos \vartheta, \varphi) = \frac{3}{4\pi} \left(\rho_{11}^1 \sin^2 \vartheta + \rho_{00}^1 \cos^2 \vartheta - \sqrt{2}\text{Re}\rho_{10}^1 \sin 2\vartheta \cos \varphi - \rho_{1-1}^1 \sin^2 \vartheta \cos 2\varphi \right)$$

$$W^2(\cos \vartheta, \varphi) = \frac{3}{4\pi} \left(\sqrt{2}\text{Im}\rho_{10}^2 \sin 2\vartheta \sin \varphi + \text{Im}\rho_{1-1}^2 \sin^2 \vartheta \sin 2\varphi \right)$$

Previous Measurements

SLAC, Ballam *et al.* [Phy. Rev. D, 7 (1973) 3150] $\rho(770)$

- Few thousand events, 7 bins in t
- s -channel helicity conservation:
 $\rho_{1-1}^1 = -\text{Im}\rho_{1-1}^2 = 0.5$
in helicity frame, all others = 0
- Parity asymmetry:
 $P_\sigma = 2\rho_{1-1}^1 - \rho_{00}^1$
- Dominated by natural parity exchange
 $P = (-1)^J$

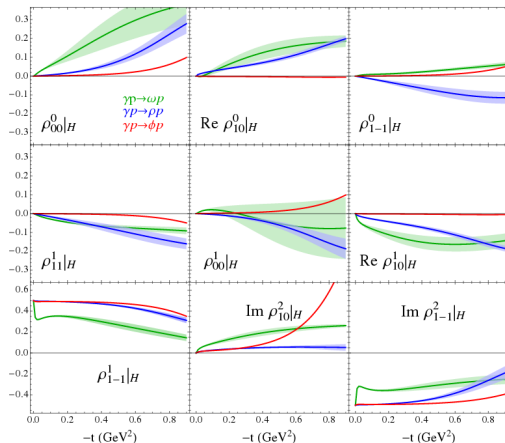
 $\omega(782)$

- Several hundred events, 3 bins in t

 $\phi(1020)$

- Few hundred events, not binned in t

JPAC Model



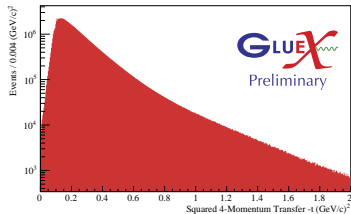
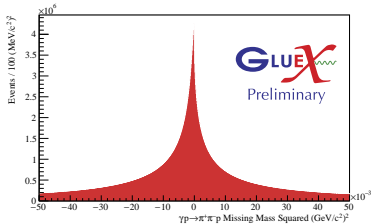
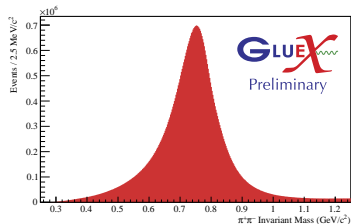
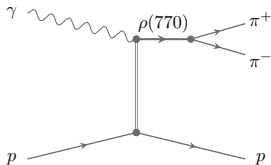
- Regge model, fit to SLAC data
- Detailed prediction for t -dependence of ρ , ω and ϕ meson production
- s -channel helicity conservation at $t = 0$



Mathieu *et al.* [Phy. Rev. D, 97 (2018) 094003]
 → Single and Double Meson Production at JLab
 (Tuesday)

Vector-Meson Photoproduction

$$\gamma p \rightarrow \rho(770) p$$



- Full 2017 data: >10M signal events in each of the 4 orientations

Extraction of SDMEs

$$W(\cos \vartheta, \varphi, \Phi) = W^0(\cos \vartheta, \varphi) - P_\gamma \cos(2\Phi) W^1(\cos \vartheta, \varphi) - P_\gamma \sin(2\Phi) W^2(\cos \vartheta, \varphi)$$

Measured Intensity $I(\Omega) \propto W(\cos \vartheta, \varphi, \Phi)$

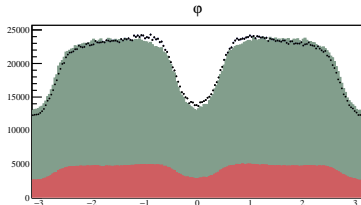
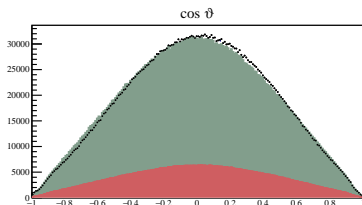
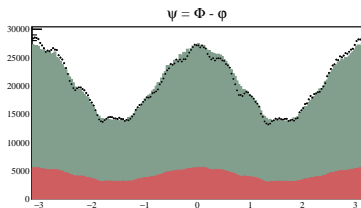
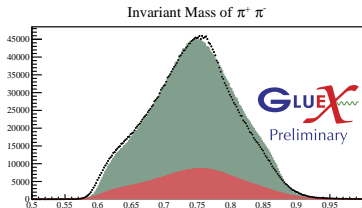
Extended Maximum-Likelihood Fit

$$\ln L = \underbrace{\sum_{i=1}^N \ln I(\Omega_i)}_{\text{Signal Events}} - \underbrace{\sum_{j=1}^M \ln I(\Omega_j)}_{\text{Background}} - \underbrace{\int d\Omega I(\Omega) \eta(\Omega)}_{\text{Normalization Integral}}$$

- Maximize by choosing SDMEs such that the intensity fits the observed N events
- Accidental background subtracted in likelihood
- Normalization integral evaluated by a phase-space Monte Carlo sample with the acceptance $\eta(\Omega) = 0/1$

Fit Evaluation

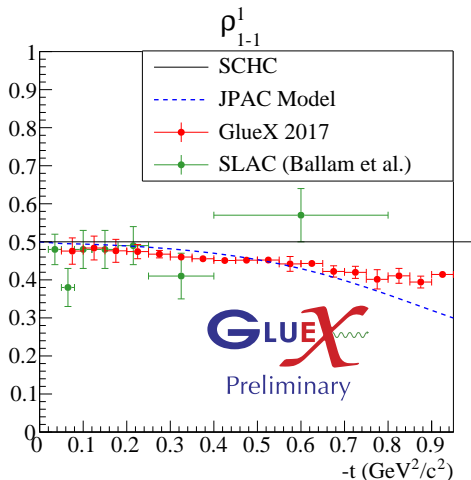
$$\gamma p \rightarrow \rho(770)p, \quad -t \in [0.05, 0.15] \text{ GeV}^2/c^2$$



- **black**: measured distribution
- **green**: accepted MC, weighted with fit result
- **red**: accidental background

Result in Bins of Momentum Transfer t

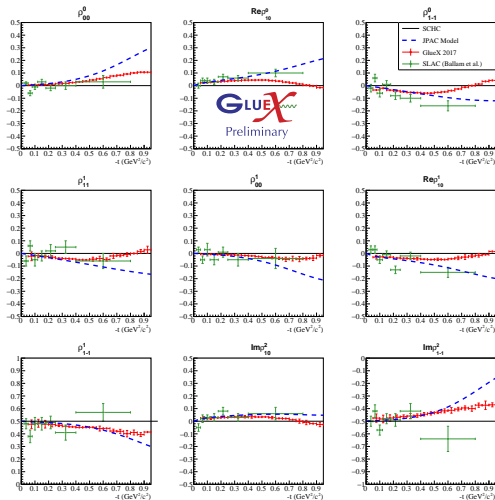
$$\gamma p \rightarrow \rho(770)p$$



- 0.05 GeV^2/c^2 bin width in t
- Average of 4 orientations
- Errors dominated by systematics
- SCHC valid for $t \rightarrow 0 \text{ GeV}^2/c^2$
- Agree with JPAC to $\sim 0.5 \text{ GeV}^2/c^2$

Result in Bins of Momentum Transfer t

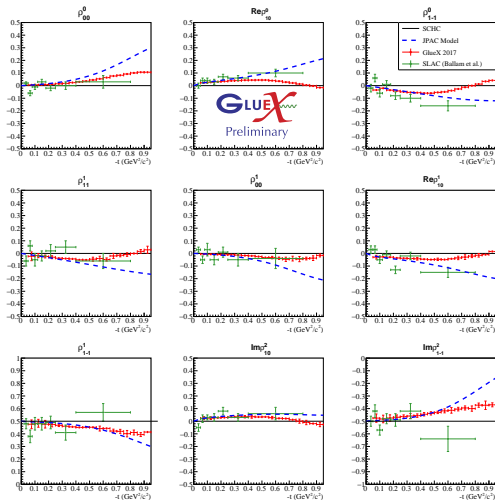
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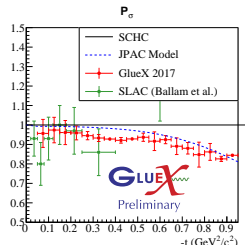
- $0.05 \text{ GeV}^2/c^2$ bin width in t
- Average of 4 orientations
- Errors dominated by systematics
- SCHC valid for $t \rightarrow 0 \text{ GeV}^2/c^2$
- Agree with JPAC to $\sim 0.5 \text{ GeV}^2/c^2$

Result in Bins of Momentum Transfer t

$$\gamma p \rightarrow \rho(770)p$$

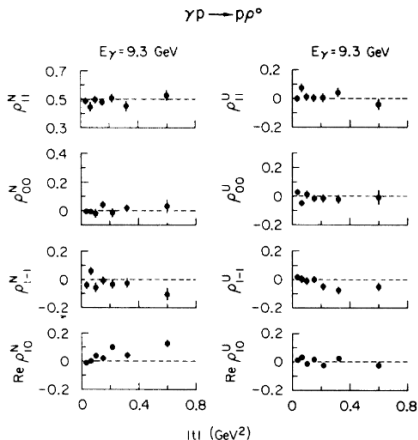


- 0.05 GeV²/c² bin width in t
- Average of 4 orientations
- Errors dominated by systematics
- SCHC valid for $t \rightarrow 0$ GeV²/c²
- Agree with JPAC to ~ 0.5 GeV²/c²



$$P_{\sigma} = \frac{\sigma_{N-\sigma U} - \sigma_U}{\sigma_{N+\sigma U}} = 2\rho_{1-1}^1 - \rho_{00}^1$$

Parity Exchange

Ballam *et al.* [Phy. Rev. D, 7 (1973) 3150]

Spin-density matrix can be separated in contributions from **natural** and **unnatural** parity exchange in the t channel

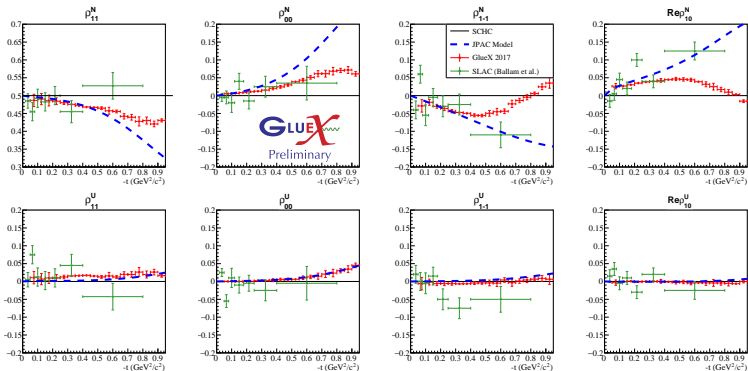
$$\rho_{ik}^{N,U} = \frac{1}{2}(\rho_{ik}^0 \mp (-1)^i \rho_{-ik}^1)$$

Schilling *et al.* [Nucl. Phys. B, 15 (1970) 397]

Only significant contribution from ρ_{11}^N
 \Rightarrow Dominant natural parity exchange

Parity Exchange

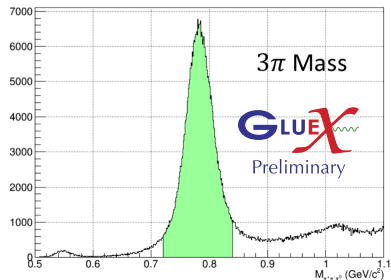
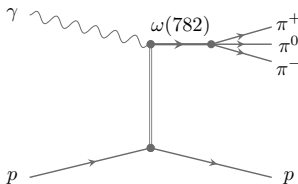
$$\gamma p \rightarrow \rho(770) p$$

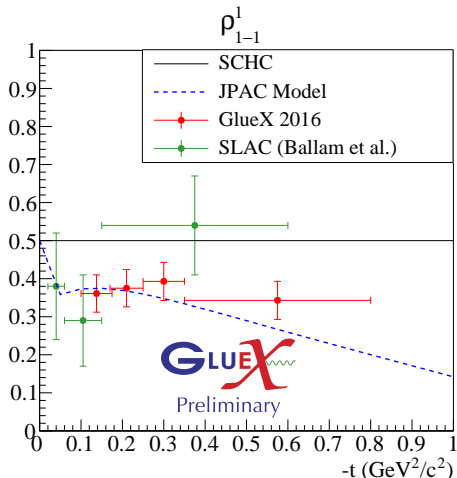


- Good agreement with JPAC for natural parity exchange at below $0.5 \text{ GeV}^2/c^2$
- Excellent agreement for unnatural parity exchange

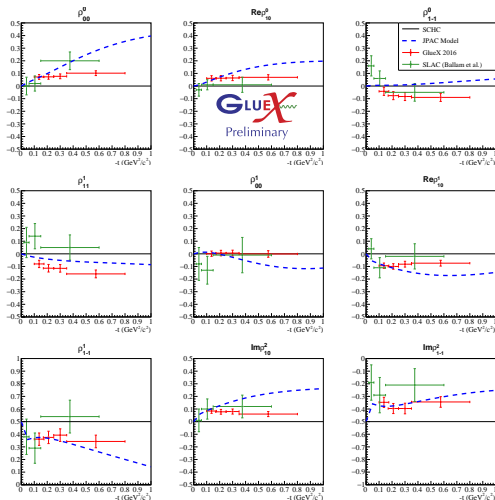
$$\gamma p \rightarrow \omega(782)p$$

$$\hookrightarrow \pi^+ \pi^- \pi^0$$

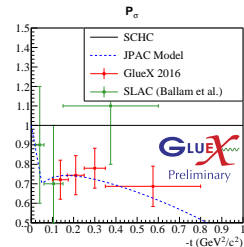


$\omega(782)$ SDMEs

- Only data of commissioning run
- 4 t bins in $[0.1, 0.8] \text{ GeV}^2/c^2$
- Average of 2 orientations
- Good agreement with prediction
- Radiative decay also analyzed

$\omega(782)$ SDMEs

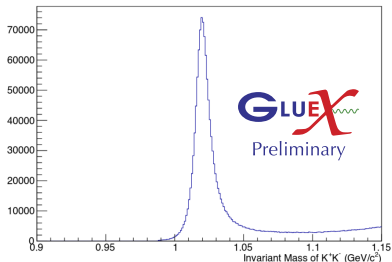
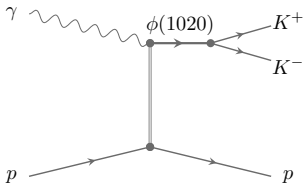
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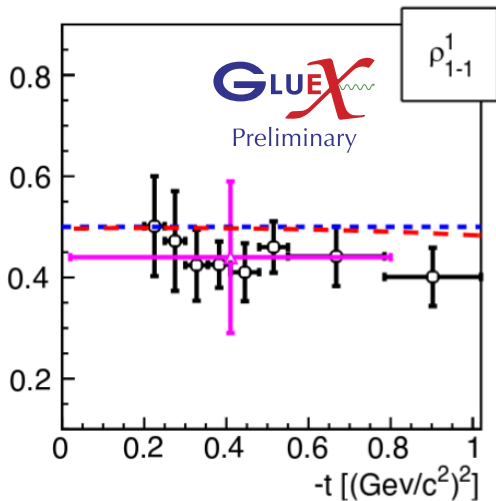


$$P_{\sigma} = \frac{\sigma_{N-} - \sigma_U}{\sigma_{N+} + \sigma_U} = 2\rho_{1-1}^1 - \rho_{00}^1$$

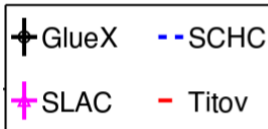
$$\gamma p \rightarrow \phi(1020)p$$

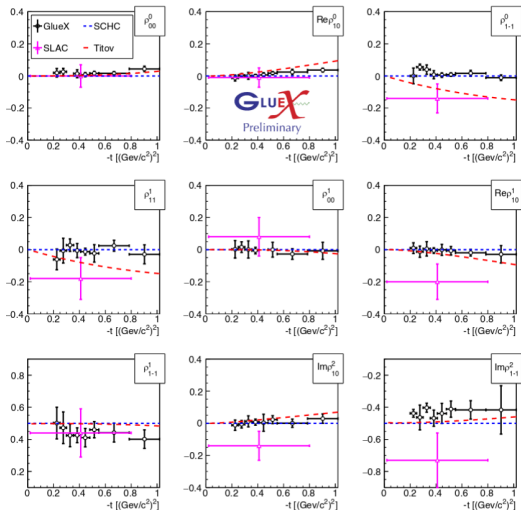
$$\downarrow K^+ K^-$$



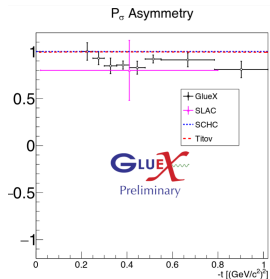
$\phi(1020)$ SDMEs

- Only fraction of 2017 data
- 8 t bins in $[0.2, 1.0] \text{ GeV}^2/c^2$
- Average of 4 orientations
- Good agreement with model
Titov *et al.* [Phys. Rev. C 60 (1999) 035205]



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- 8 t bins in $[0.2, 1.0] \text{ GeV}^2/c^2$
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$$P_{\sigma} = \frac{\sigma_N - \sigma_U}{\sigma_N + \sigma_U} = 2\rho_{1-1}^1 - \rho_{00}^1$$

Summary and Outlook

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- Spin-density matrix elements extracted for $\rho(770)$, $\omega(782)$ and $\phi(1020)$
- Statistical precision increased by **orders of magnitude**
- **Natural parity exchange** dominates at $E_\gamma = 9 \text{ GeV}$ for $t \rightarrow 0$
- General agreement with models for $t \lesssim 0.5 \text{ GeV}^2/c^2$
- Analysis also used to tune and confirm MC simulation

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- General agreement with models for $t \lesssim 0.5 \text{ GeV}^2/c^2$
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Outlook

- Full GlueX-I data set will be available this summer
- Results serve as input to **improved model** of production process
- Prerequisite for **interpretation of exotic signals**