

Measuring the Polarizability of the Neutral Pion with GlueX

Proposal to run concurrently with
"Measuring the Charged Pion Polarizability (CPP)
in the $\gamma\gamma \rightarrow \pi^+ \pi^-$ Reaction"
E12-13-008

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Internal GlueX review

- Conclusion and summary from the *ad hoc* Review:
 - NPP is compatible with CPP
 - The proposed measurements were feasible in the beam time requested.

This experiment has been endorsed by the GlueX collaboration

Polarizability

- Polarizability: Ease with which an external field induces a dipole moment in a particle and is a property that reflects the internal structure of the particle
- The π^0 polarizability has NEVER been measured

$$\alpha_{\pi^+} = 2.0 \pm 0.9 \times 10^{-4} \text{fm}^3 \quad (\text{CPP})$$

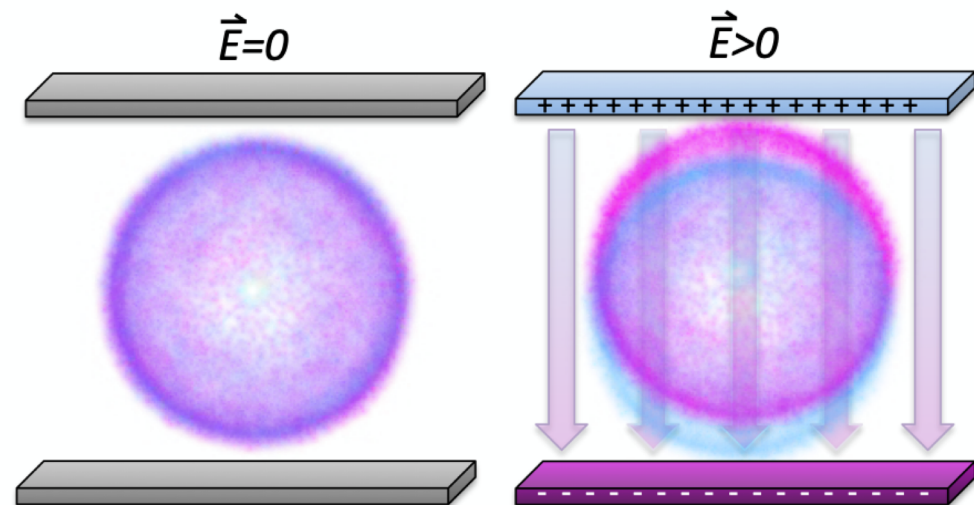
COMPASS Phys. Rev. Lett., 114 (2015) 062002

$$\alpha = -\beta$$

Lowest order in χ PT

Deviations are sensitive to two-loop calculations and meson cloud dynamics

α - electric polarizability
 β - magnetic polarizability



$$\vec{p} = \alpha \vec{E}$$

$$\vec{\mu} = \beta \vec{H}$$

Experimental considerations

- Requirements are similar to Charged Pion Polarizability Ex (CPP)
 - High Z target -> signal is proportional to Z^2
 - Low beam energy -> 6 GeV gives better acceptance and higher polarization
 - Accurate normalization scheme -> measure absolute cross section
- Conclusion: Run concurrently with CPP

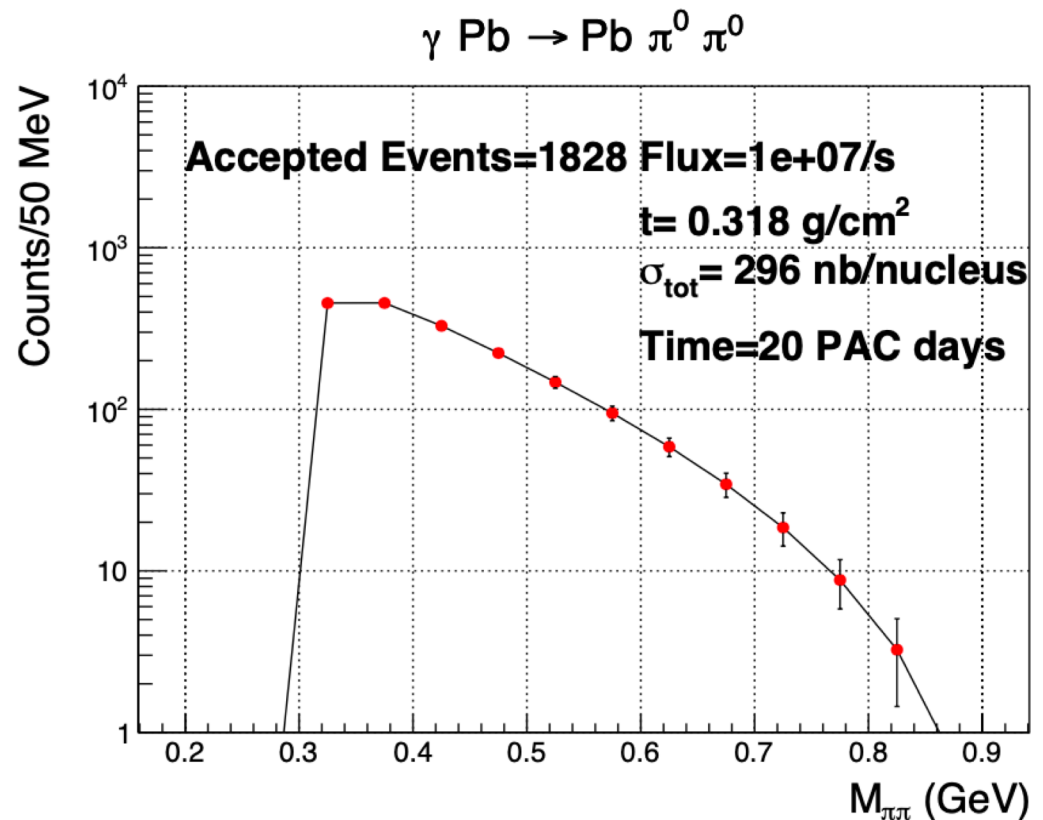
Configuration	Nominal GlueX I	Charged Pion Polarizability	Neutral Pion Polarizability
Coherent Peak Energy	8.4-9.0 GeV	5.5-6 GeV	5.5-6 GeV
Current	150 nA	20 nA	20 nA
Peak polarization	35%	72%	72%
Target Position	65 cm	1 cm	1 cm
Target	LH2, 30 cm	^{208}Pb , 0.028 cm	^{208}Pb , 0.028 cm
Muon Detector	None	Installed	Not needed
Trigger	FCAL/BCAL (40 kHz)	TOF (30 kHz)	FCAL/BCAL (10 kHz)

Note: Electron beam energy = 11.4 GeV

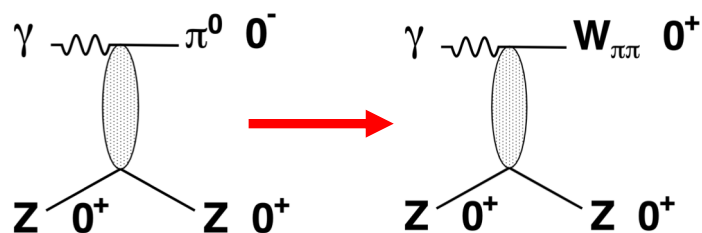
Expected signal for $\gamma \text{Pb} \rightarrow \text{Pb} \pi^0 \pi^0$

$$\frac{d^2\sigma}{d\Omega_{\pi\pi}dW_{\pi\pi}} = \frac{2\alpha Z^2 E_\gamma^4 \beta^2 \sin^2 \theta_{\pi\pi}}{\pi^2 W_{\pi\pi} Q^4} |F(Q^2)|^2 \sigma(\gamma\gamma \rightarrow \pi^0 \pi^0) (1 + P_\gamma \cos 2\phi_{\pi\pi}).$$

- Number of events estimated based on the Crystal Ball measurement
- Use CPP flux, target, running time, detector acceptance
- 20 PAC days
- Total signal events: 1800



Expected backgrounds



Integrated Fraction ($\theta < 1.5$ degrees)	$\gamma Pb \rightarrow \pi^0 Pb$	$\gamma Pb \rightarrow \pi^0 \pi^0 Pb$ (This study)
Primakoff signal	1.0	1.0
Nuclear Coherent (NC)	0.39	0.35
Interference	0.12	0.17
$\gamma p \rightarrow \eta p$, BR($\eta \rightarrow 3\pi^0$)	–	0.37
Incoherent (IC)	0.02	0.06

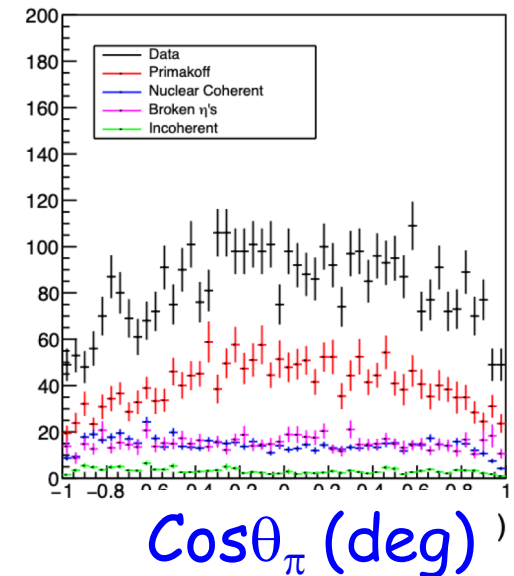
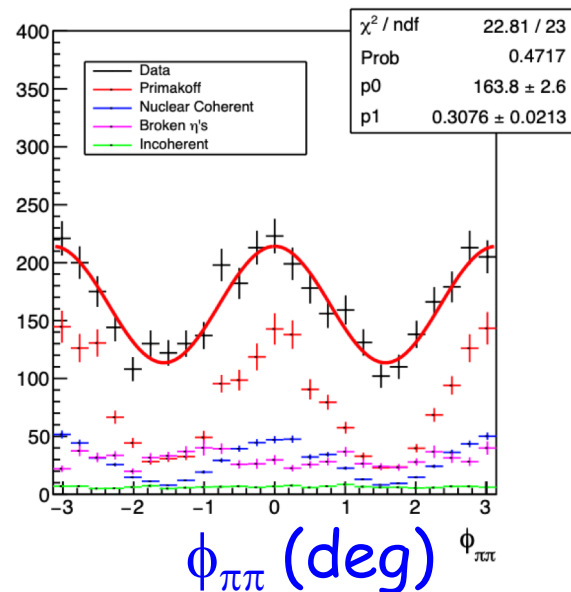
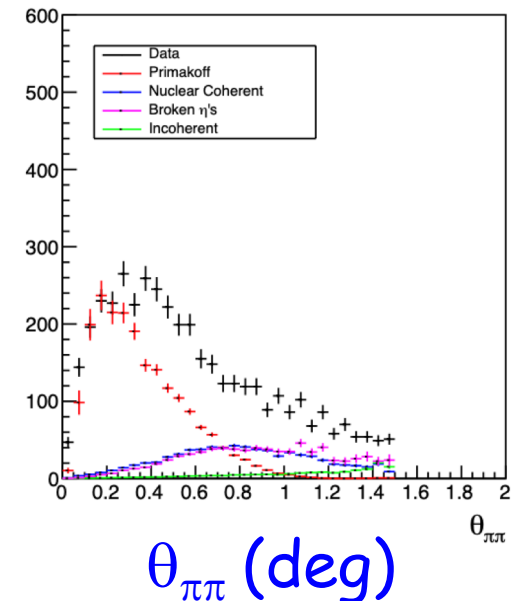
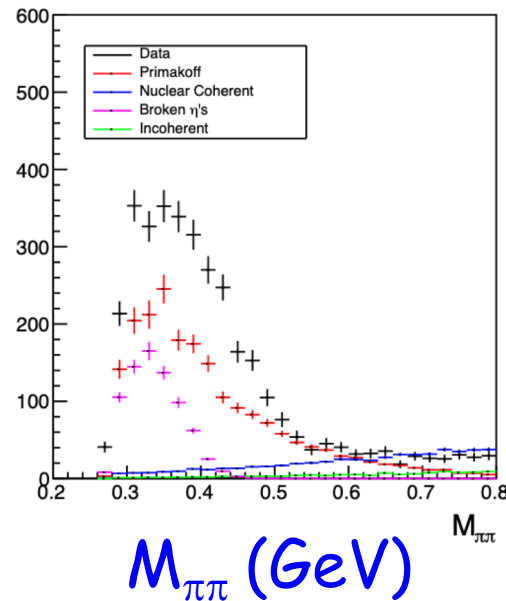
- Nuclear Coherent production (e.g. $f_0(500) \rightarrow \pi^0 \pi^0$)
 - π^0 's produced in the NC production are suppressed by Pauli blocking and absorption. Suppression is seen in PrimEx- π^0 , expect stronger suppression in $\pi^0 \pi^0$
 - Adjusted NC and Interference to approximately match PrimEx
- Misidentified backgrounds
 - Nuclear coherent η production: $\eta \rightarrow \pi^0 \pi^0 \pi^0 \rightarrow \gamma \gamma \gamma (\gamma \gamma)$
- Advantages: $\rho^0 \not\rightarrow \pi^0 \pi^0$, no QED background, and no pion exchange due to CP conservation.

Fit to signal and background

Full simulation with

- GEANT4
- Detector resolution
- Standard GlueX Reconstruction
- Kinematic fit
- Random hits
- Tagger accidentals

Results shown of
Amplitude fit to
all variables



Error table

	Source	Uncertainty
1	Statistical uncertainty	2.3%
2	Signal extraction	3.0%
3	Detector acceptance and efficiency	3.5%
4	Total systematic error	4.6%
5	Total error on cross section	5.1%
6	Projected error in $\alpha - \beta$	39%

Taken from fit

Compare fits
with/without misID
 η 's and IC

Assess using uncertainty
in measuring γ Pb \rightarrow π^0 Pb

Use estimate by
Dai/Pennington

$$\Delta(\alpha_{\pi^0} - \beta_{\pi^0}) \sim 7.7\Delta(\sigma)$$

Compare COMPASS result

$$\alpha_{\pi^+} - \beta_{\pi^+} = 4 \pm 1.8 \times 10^{-4} \text{fm}^3$$

Projected CPP rounded theory estimate for value

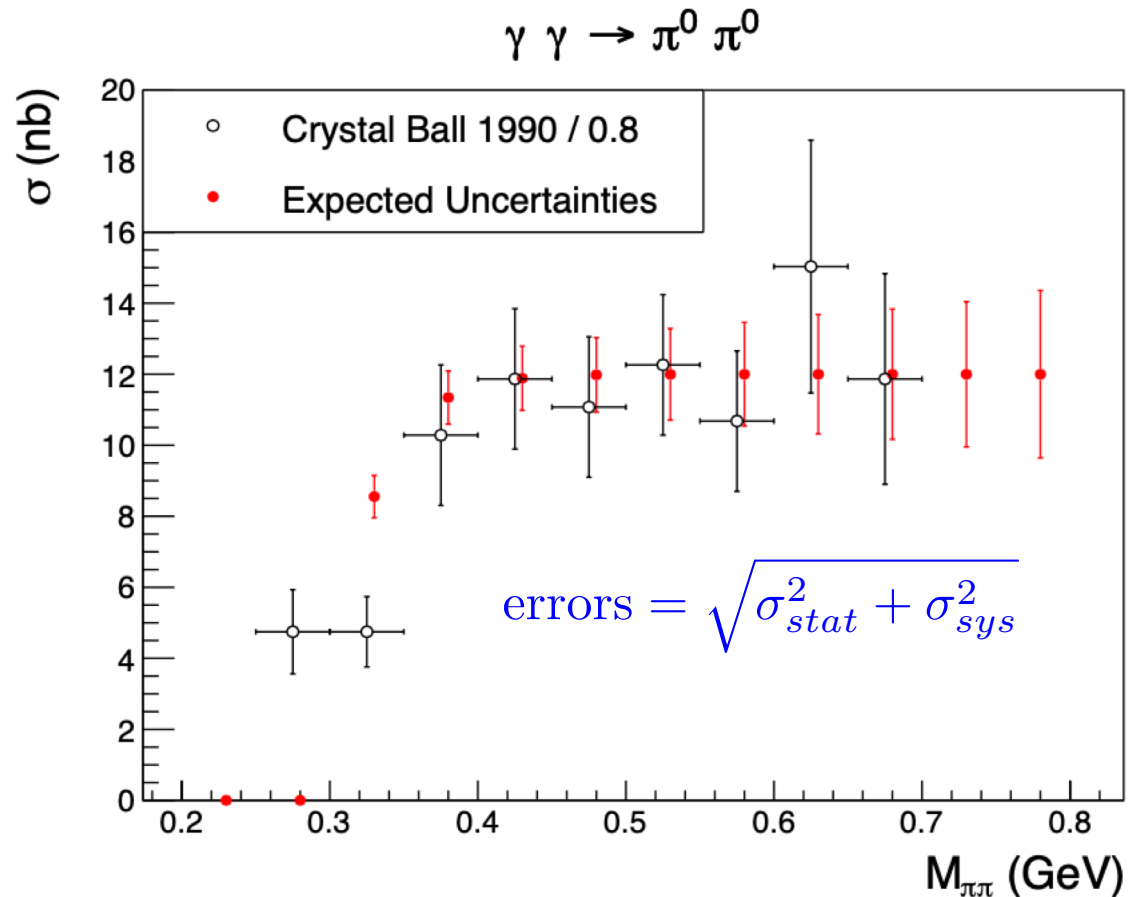
$$\alpha_{\pi^+} - \beta_{\pi^+} \sim 6 \pm 0.6 \times 10^{-4} \text{fm}^3$$

Projected NPP rounded theory estimate for value

$$\alpha_{\pi^0} - \beta_{\pi^0} \sim -2 \pm 0.8 \times 10^{-4} \text{fm}^3$$

Sensitivity

- High sensitivity of experiment at low $W_{\pi\pi}$
- Dai and Pennington: 5.1% determination of $\sigma(\gamma\gamma \rightarrow \pi^0\pi^0)$ gives $\alpha_\pi - \beta_\pi$ to 39%
- Best analysis uses combination of χ PT and dispersion relation analysis
- Cross section measurement as a function of $W_{\pi\pi}$ is of general theoretical interest



Summary and outlook

- **NPP will measure the π^0 polarizability for the first time**
- Pion polarizabilities are sensitive tests of their Goldstone Boson nature. **There is keen theoretical interest and excellent support**

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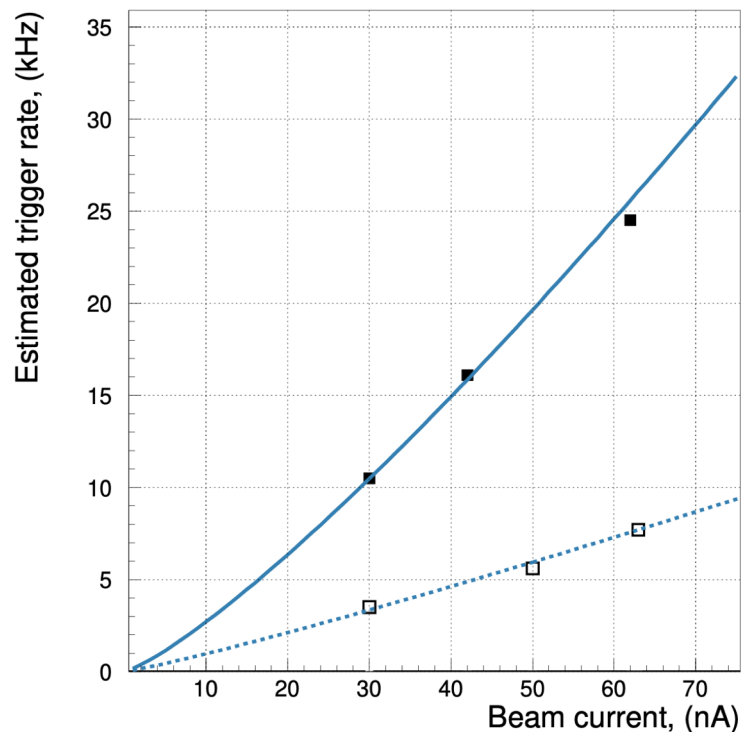
S. Gevorkyan, *Joint Institute for Nuclear Research, Dubna, Russia*

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- **We have simulated the primary backgrounds expected in the experiment**
 - Nuclear coherent
 - Misidentified $\eta \rightarrow \pi^0 \pi^0 \pi^0$
 - Incoherent production
- We estimate we will measure the cross section $\sigma(\gamma\gamma \rightarrow \pi^0 \pi^0)$ with an uncertainty of 5.1%, leading to an uncertainty on the neutral pion polarizability for $\alpha-\beta$ of 39%.
- The projected absolute uncertainty is similar to uncertainties for measurements of the polarizabilities of charged pions and the proton.

Compatibility with CPP

- Target for CPP and NPP will be ^{208}Pb
 - This decision was made for CPP after PAC approval
- Rate for neutral trigger is < 10 kHz ($E_{\text{FCAL}} > 1$ GeV), which will allow running concurrently with CPP

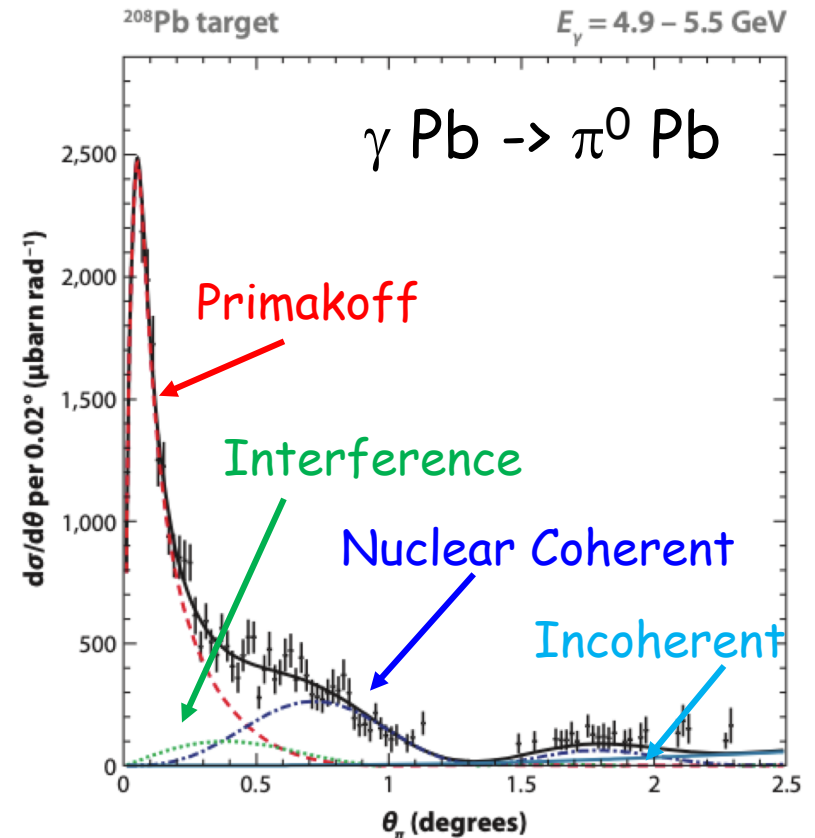


- Scale measured rates during test to CPP conditions:
 - Current = 20 nA
 - Target = 5% Rad. Length
 - Trigger rate < 10 kHz

Review: single p_0 production (PrimEx)

Ann Rev Nucl Part Sci 61 (2011) 1

- **Primakoff** production (photon-exchange mechanism). Peaks at 0.02°
- **Nuclear Coherent** production (vector-meson exchange mechanism). Peaks at $\sim 0.75^\circ$.
- **Interference** between Primakoff and Nuclear Coherent.
- **Incoherent** production $\gamma N \rightarrow N \pi^0 \pi^0$. Peaks at large angle and high $W_{\pi\pi}$

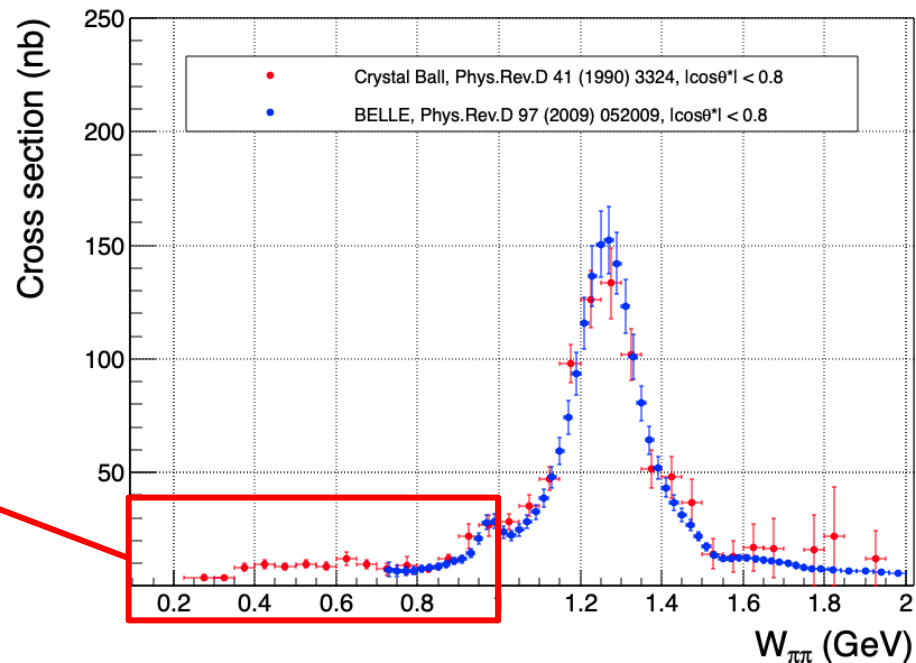
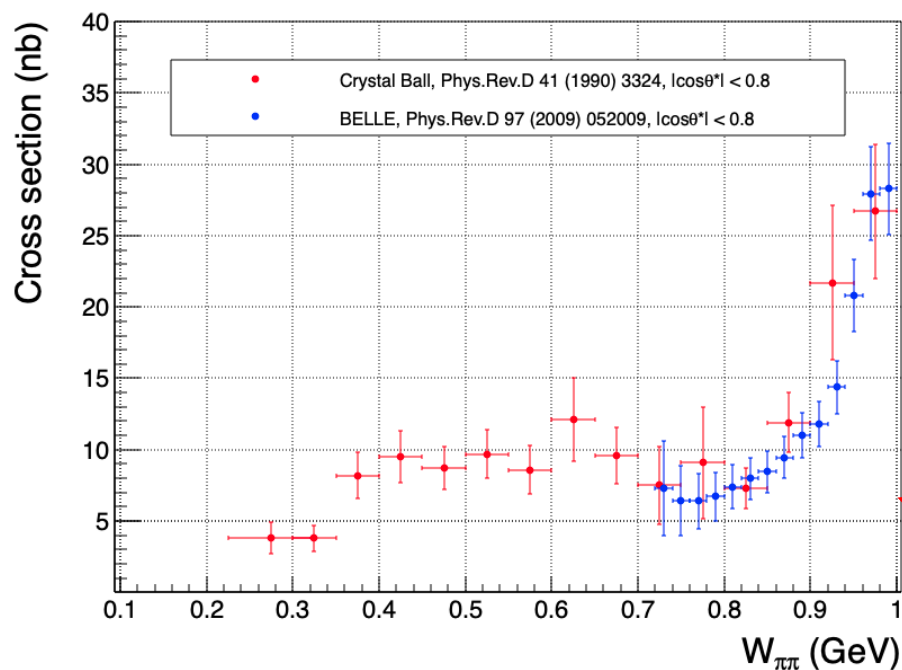


Past measurements (e+e-)

$$\gamma\gamma \rightarrow \pi^+\pi^-$$

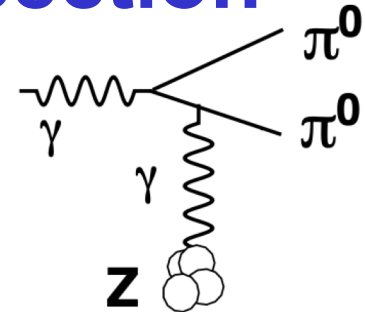
- Crystal Ball at DESY (DORIS II), 1990 [$W_{\pi\pi} < 0.6 \text{ GeV}$]
- BELLE at KEK (KEKB), 2009 [$0.7 < W_{\pi\pi} < 4.0 \text{ GeV}$]
- Cross section at low $W_{\pi\pi}$ is poorly known

Threshold Region



Polarizabilities $\rightarrow \chi\text{PT} \rightarrow$ dispersion relations \rightarrow cross section

$$\gamma Pb \rightarrow (Pb) \pi^0 \pi^0$$



- The polarizabilities are defined in terms of the forward Compton Amplitudes ($\gamma\pi^0 \rightarrow \gamma\pi^0$).
- Extrapolation is needed to relate these amplitudes to the measured ($\gamma\gamma \rightarrow \pi^0\pi^0$) cross section
- χPT provides the connection between the polarizability and spontaneous chiral symmetry breaking, but χPT is perturbative and diverges at high momentum.
- Dispersion Relations provide bridge between low and high $W_{\pi\pi}$
- Extraction of polarizabilities from the experimental cross section requires Dispersion theory matched with chiral perturbation theory.

Theory support

- Significant theoretical interest in a ~40% measurement of the neutral pion polarizability (-> 5% uncertainty of cross section)
- Theory involves the use of dispersion relations supplemented with chiral perturbation theory, which together permits an extrapolation of the Compton amplitudes from the $\gamma \gamma \rightarrow \pi^0 \pi^0$ to the $\gamma \pi^0 \rightarrow \gamma \pi^0$ channel.
- Two-loop corrections will be significant; methodology is available; work is in progress
- Complimentary expertise in the theory support group: [Jose Goity](#) (JLab) and [Aleksandrs Aleksejevs](#) + [Svetlana Barkanova](#) (Memorial University of Newfoundland, Canada), [S. Gevorkyan](#) (Joint Institute for Nuclear Research, Dubna, Russia), [L.-Y. Dai](#) (Hunan University, China)

Detector resolution

$$\sigma_{M_{\pi\pi}} = 12 \text{ MeV}$$

$$\sigma_{\theta} = 0.1 \text{ deg}$$

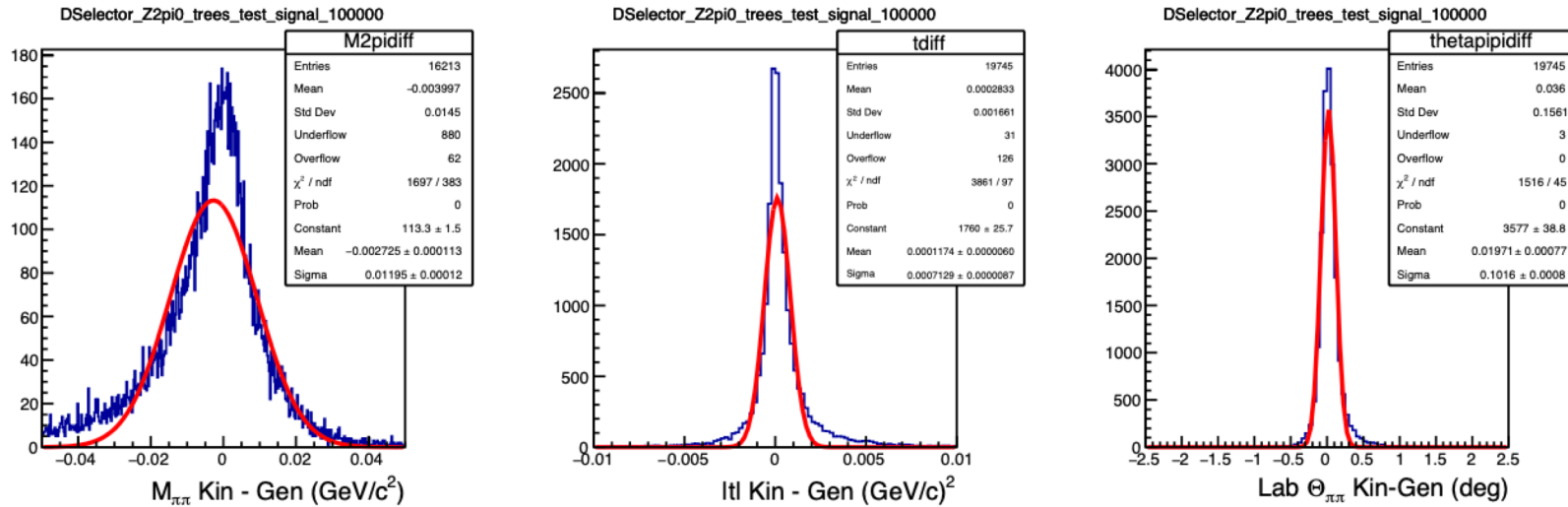


Figure 11: Left: Difference between kinematically fit and generated 2π mass. The central 2π -mass σ is about 12 MeV. Center: Difference between kinematically fit and generated $-t$. Right: Difference between kinematically fit and generated 2π polar angle. The resolution σ of the reconstructed angle is 0.1 degrees.