

# Kinematic Fitting in GlueX

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- started looking into kinematic fit code (DKinFit)
- found some issues, possible improvements
- possible bug in translation of tracking matrix into kinematic fit matrix

# DKinFit class

- based on CLAS kinematic fit code (CMU)
- written by Matt Bellis, Mike Williams
- the CLAS kfit code has been used in various publications by CMU
- rather straightforward to use
- went through the entire code, did not see anything that seemed different from the CLAS code
- documentation available at (CLAS note)  
[http://www.jlab.org/Hall-B/notes/clas\\_notes03/03-017.pdf](http://www.jlab.org/Hall-B/notes/clas_notes03/03-017.pdf)

# Implementing DKinFit (1/2)

```
DKinFit *kfit = new DKinFit();  
kfit->ResetForNewFit();  
kfit->SetVerbose(1);  
kfit->SetInitial(kd_initialStateIn);  
kfit->SetFinal(kd_initialStateOut);  
// kfit->SetMissingParticle(0);  
kfit->Fit();
```

vector of DKinematicData



specify mass of missing particle,  
comment out if no missing particle



# Implementing DKinFit (2/2)

- can pull out various quantities, such as  $\chi^2$ , ndf,

pulls for each variable

```
chi2 = kfit->Chi2();
```

```
ndf = kfit->Ndf();
```

```
CL = TMath::Prob(chi2,ndf);
```

```
pull = kfit->GetPull(n);
```

nth pull

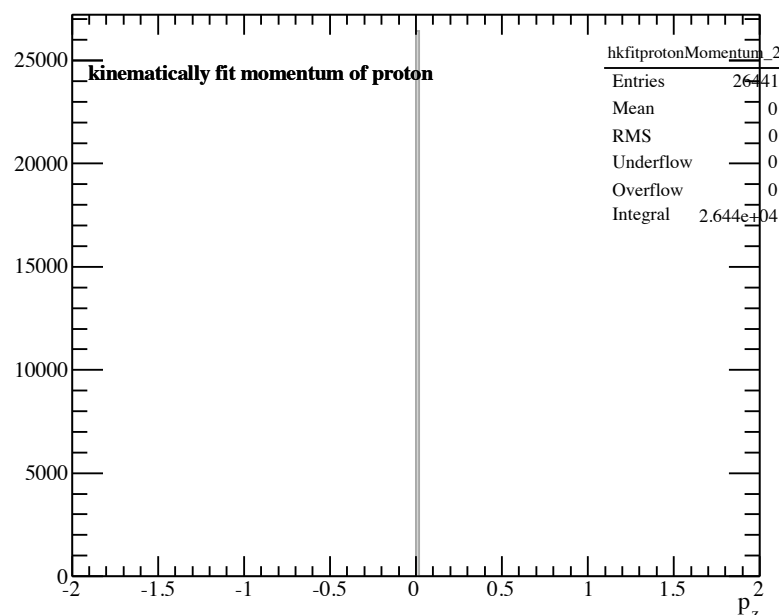
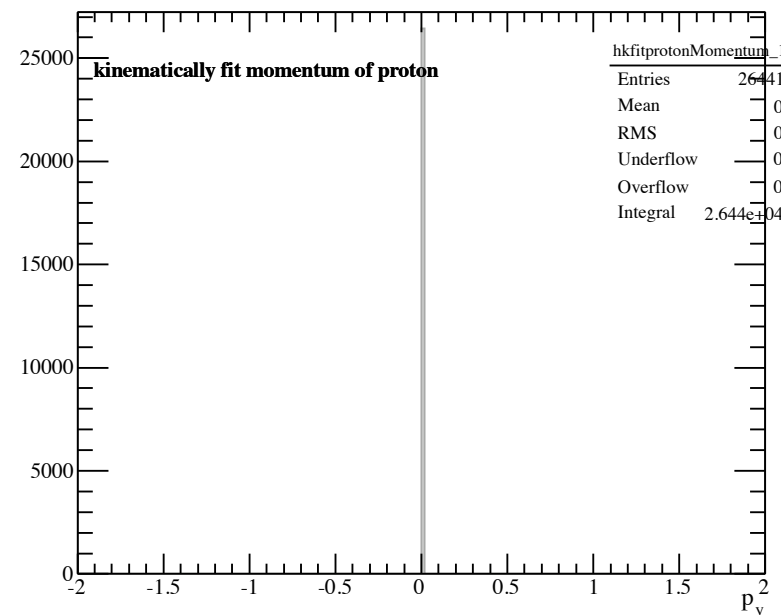
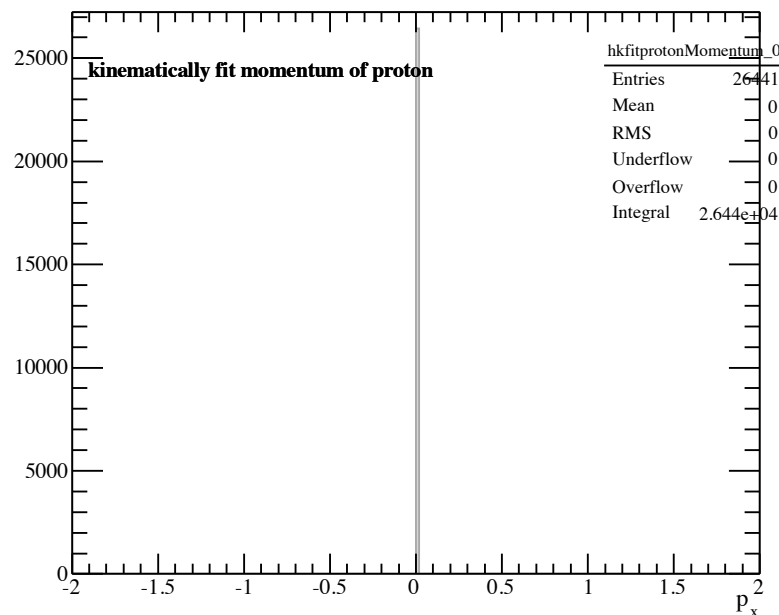


# Initial State

1. smearing of initial momenta is done by `smearMCThrownMomentum(smear)`
2. smear momentum around original value by smear, and updates error
3. this function does NOT do anything if original momentum is 0.
4. if this is the case, there is NO wiggle room for these variables since the error matrix is 0.
5. in the future, we should probably think of what to do with the error on the initial photon, in relation with the tagger.

# Fitting to $p \pi^+ \pi^-$

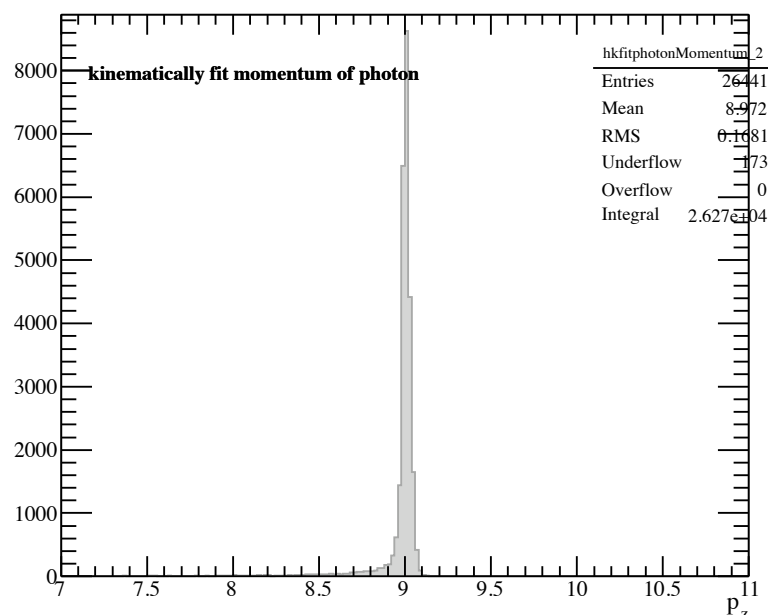
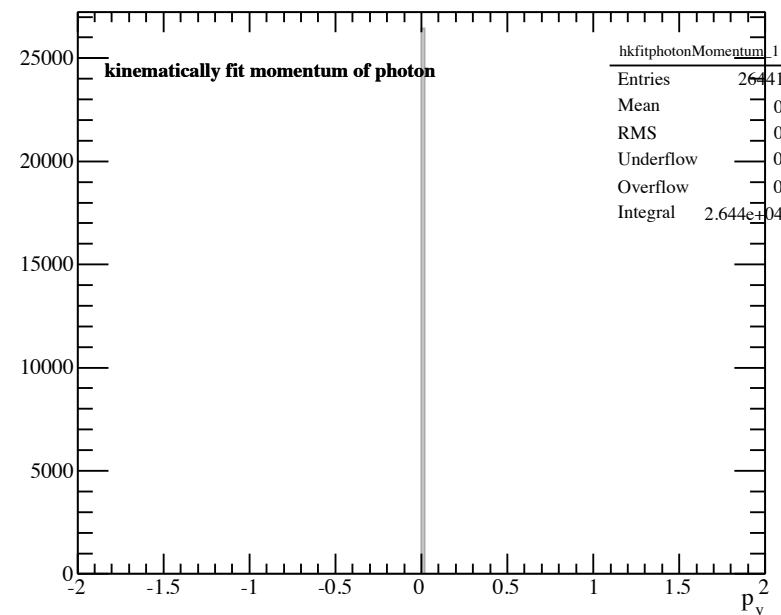
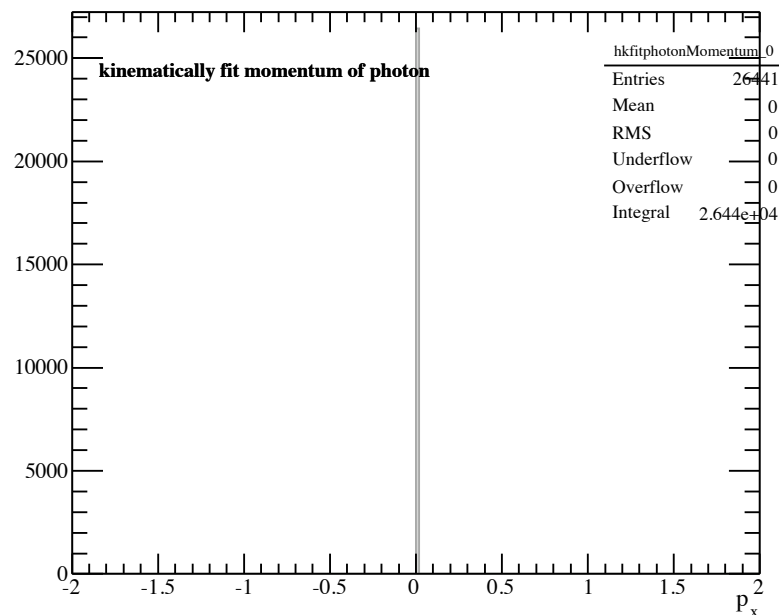
1. try fitting to exclusive  $p \pi^+ \pi^-$  events.
2. generate using genr8, process through hdgenat, then reconstruction



momentum of kfit initial proton does not change from 0 since the error matrix is 0

# Fitting to $p \pi^+ \pi^-$

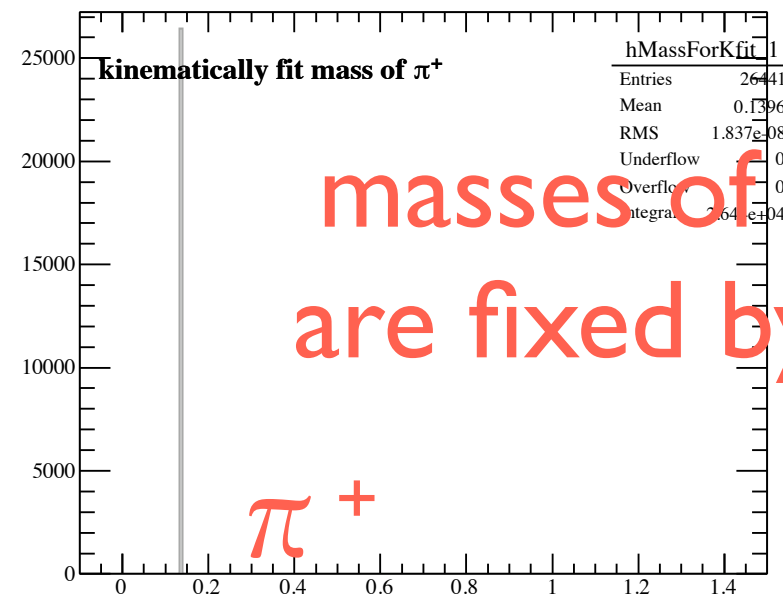
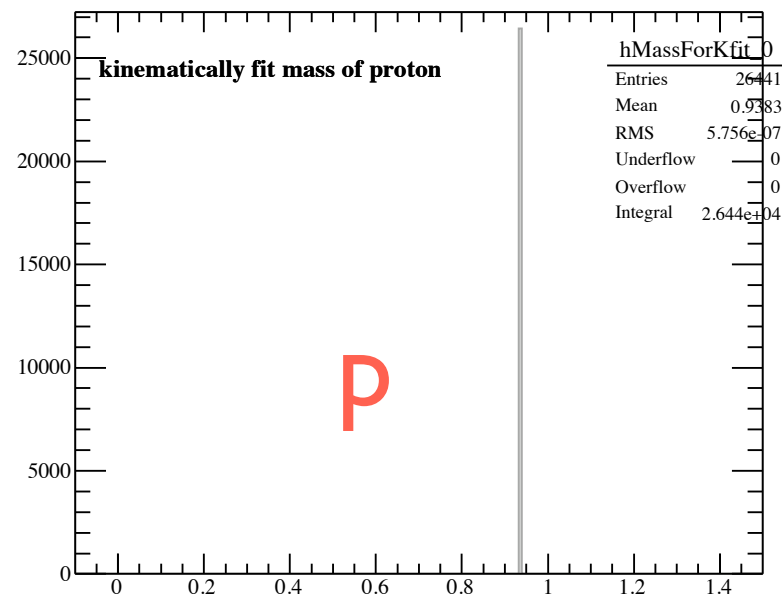
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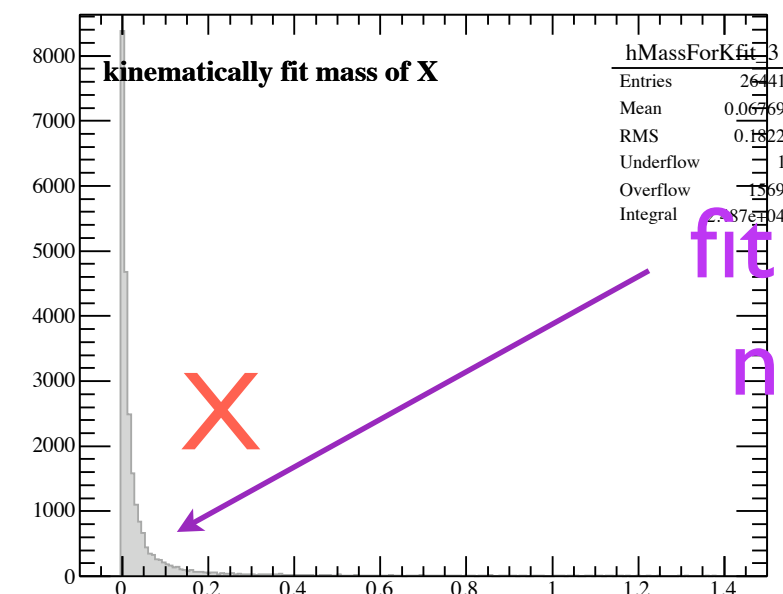
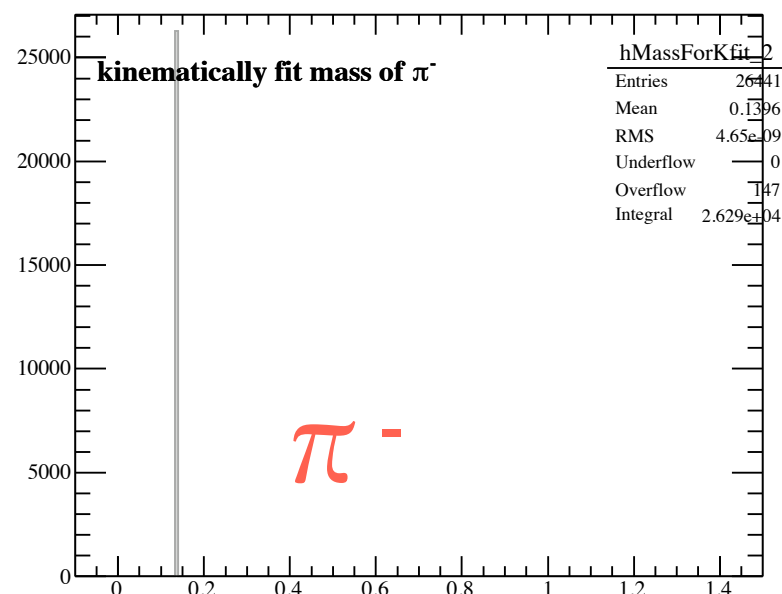
momentum of kfit initial photon changes in the z-direction (used smear of 0.001)

# Fitting to $p \pi^+ \pi^-$

1. try fitting to exclusive  $p \pi^+ \pi^-$  events.
2. generate using genr8, process through hdgenat, then reconstruction



masses of final particles are fixed by kinematic fit



fit probably did not converge

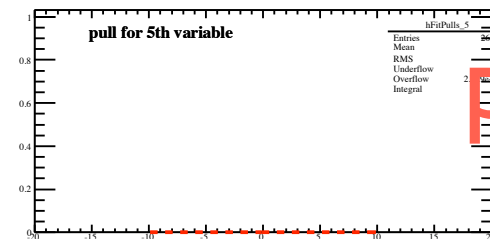
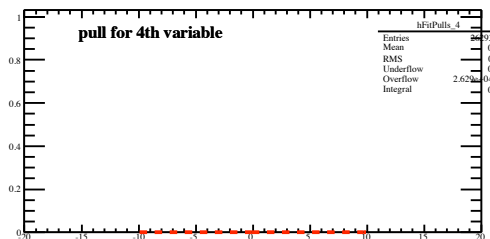
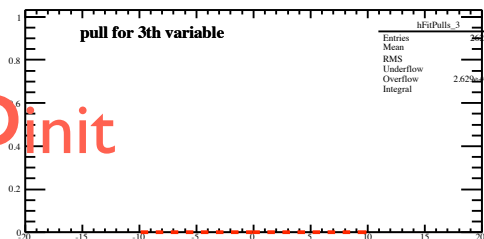
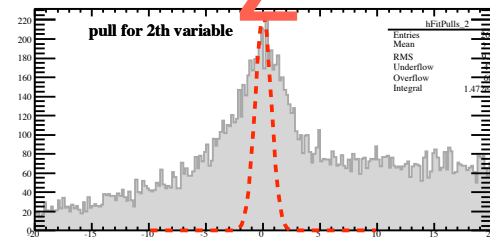
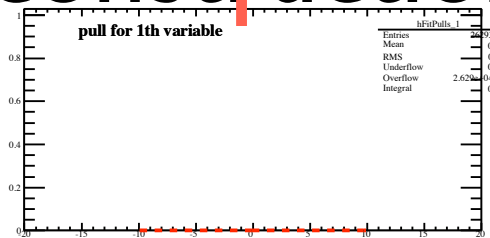
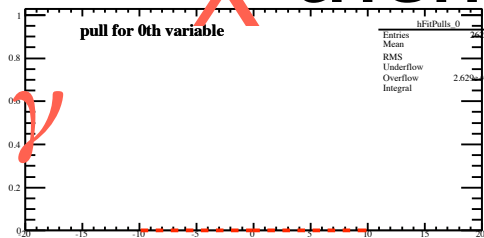


# Fitting to $p \pi^+ \pi^-$

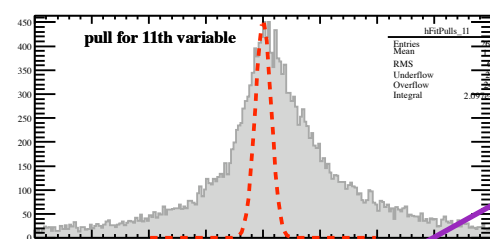
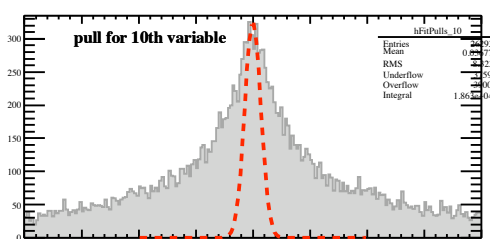
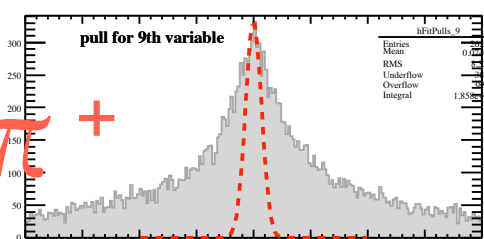
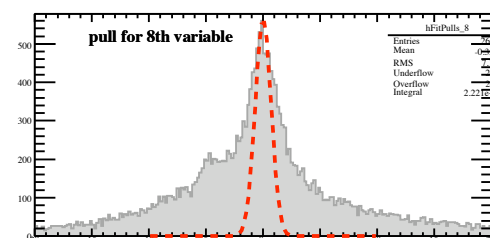
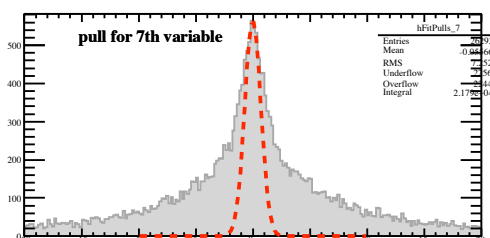
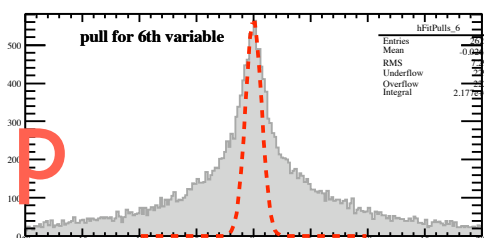
1. try fitting to exclusive  $p \pi^+ \pi^-$  events.

2. generate using genr8, process through hdgenat,

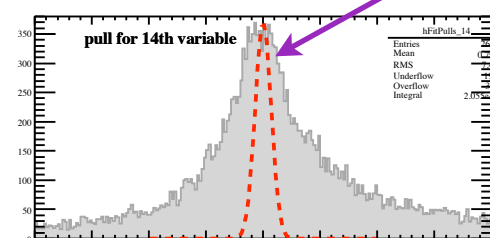
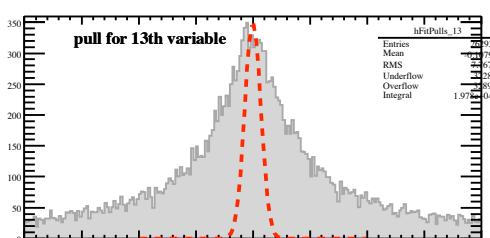
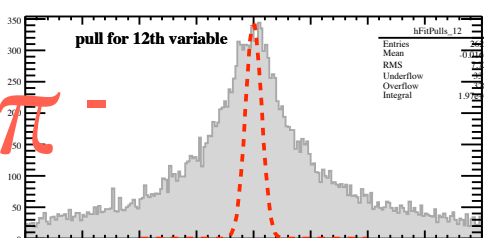
~~X~~ then reconstruction



pulls of each variable

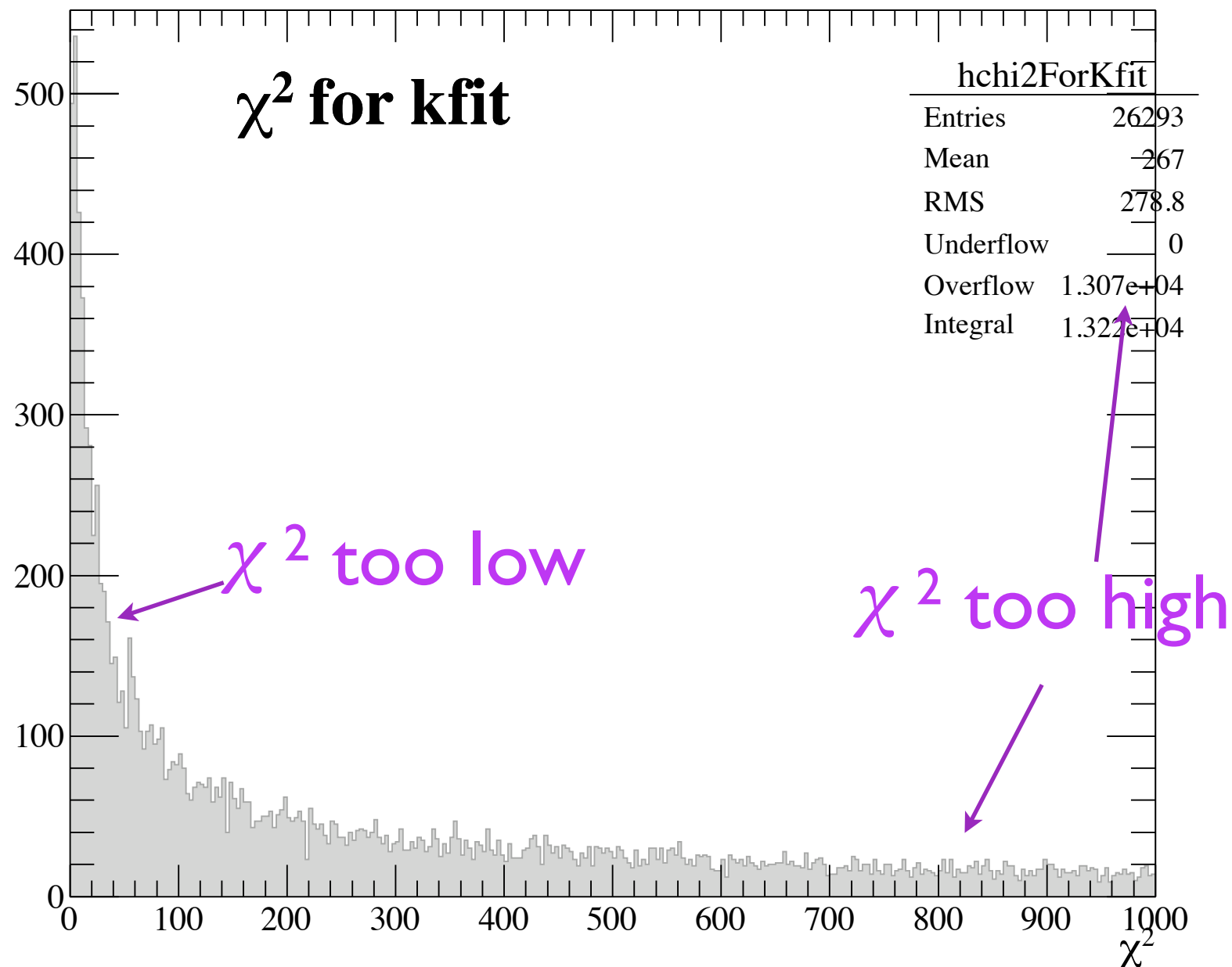


Gaussians normalized to same height



# Fitting to $p \pi^+ \pi^-$

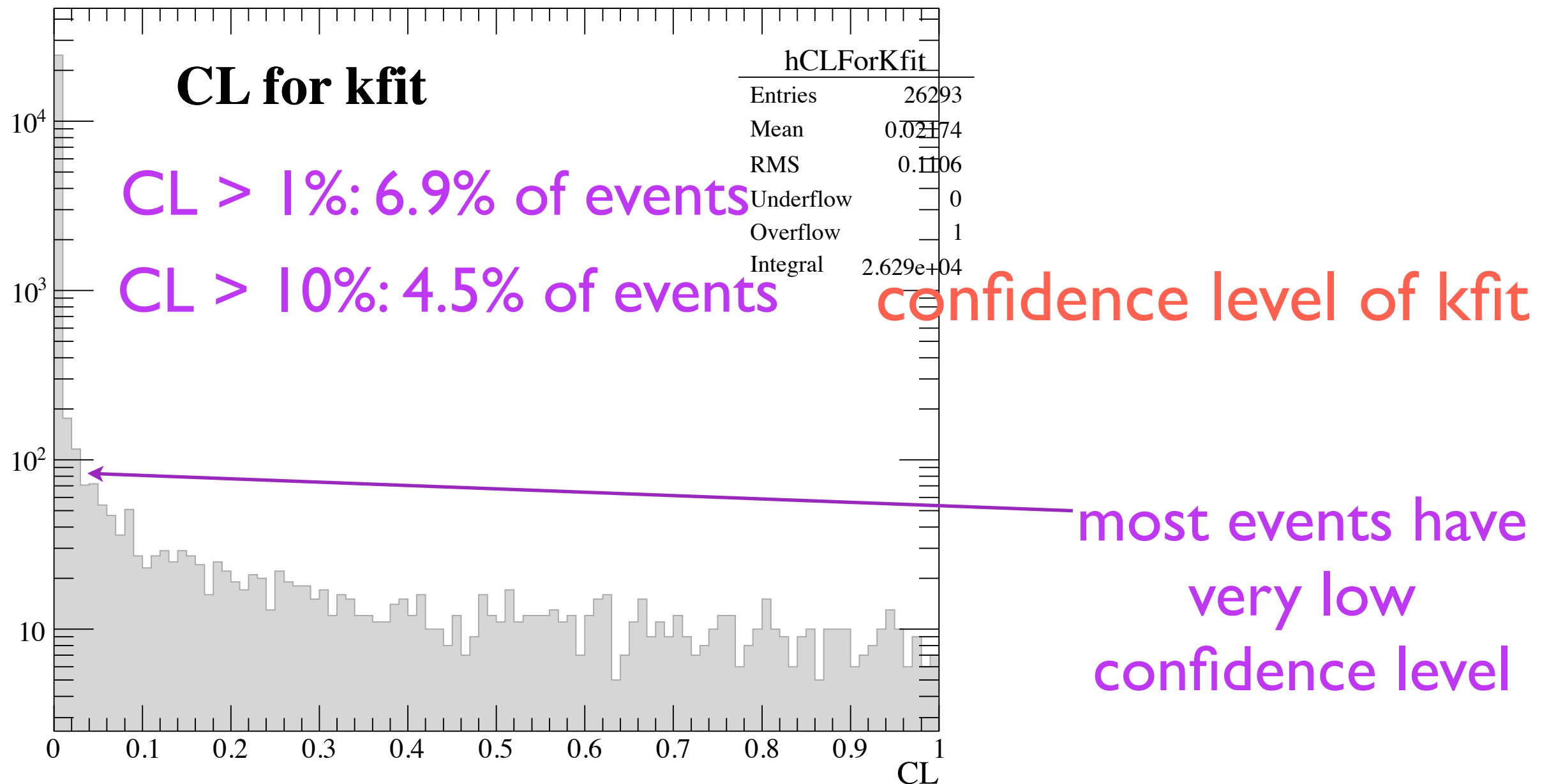
1. try fitting to exclusive  $p \pi^+ \pi^-$  events.
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$\chi^2$  of kfit  
(ndf = 4)

# Fitting to $p \pi^+ \pi^-$

1. try fitting to exclusive  $p \pi^+ \pi^-$  events.
2. generate using genr8, process through hdgenat, then reconstruction



# Possible Improvements

1. set up flag for convergence
2. fitting to neutrals?
3. function that returns how many pulls are available
4. function that uses timing information to add extra degrees of freedom is available, but have not looked into this yet.
5. setting of covariance matrix for missing particle is in CLAS coordinates, meaningless.

# Error Matrices

1. Errors of kinematic fit are derived from error matrix of each particle, which is in the  $\{p_x, p_y, p_z, E, x, y, z\}$  (DKinematicData) basis.
2. These errors are taken from the track fitting program, where fitting is done in the  $\{q/p_T, \varphi, \tan\lambda, D, z\}$  (tracking) basis.
3. Propagation of these errors is handled in `DTrackFitterKalmanSIMD::FitTrack(void)` where the 5x5 tracking cov. matrix is converted to the 7x7 DKinematicData basis cov. matrix via  $C_{\text{DKinematicData}} = J C_{\text{tracking}} J^T$ , where  $J$  is 7x5

# Error Matrices

1. The actual code to do this is

```
fitparams.setErrorMatrix(Get7x7ErrorMatrix(errMatrix));
```

member of DTrackFitter of  
type DKinematicData which  
holds the tracking fit result

converts 5x5 tracking  
matrix into 7x7  
DKinematicData cov.  
matrix via J (7x5)

5x5 tracking  
matrix


2. The matrix J is given within the function

`DTrackFitterKalmanSIMD::Get7x7ErrorMatrix`

and each component is  $J_{ij} = \partial y_i / \partial x_j$  where  $y_i$  is in the DKinematicData basis, and  $x_j$  is in the tracking basis.


# Error Matrices

I have gone through each component of J, and think there may be two bugs:

1.  $\partial E / \partial (q/p_T)$   should be units of  $E^2$

Within the code:

`J(state_E, state_q_over_pt) = q*pt*p_sq/E3;`

 dimensionless  
should be  $-q p_T^3 (1 + \tan^2 \lambda) / E$

2.  $\partial E / \partial (\tan \lambda)$   should be units of E

Within the code:

`J(state_E, state_tanl) = pt_sq*tanl_/E3;`

should be  $p_T^2 \tan \lambda / E$

 units of  $E^{-1}$