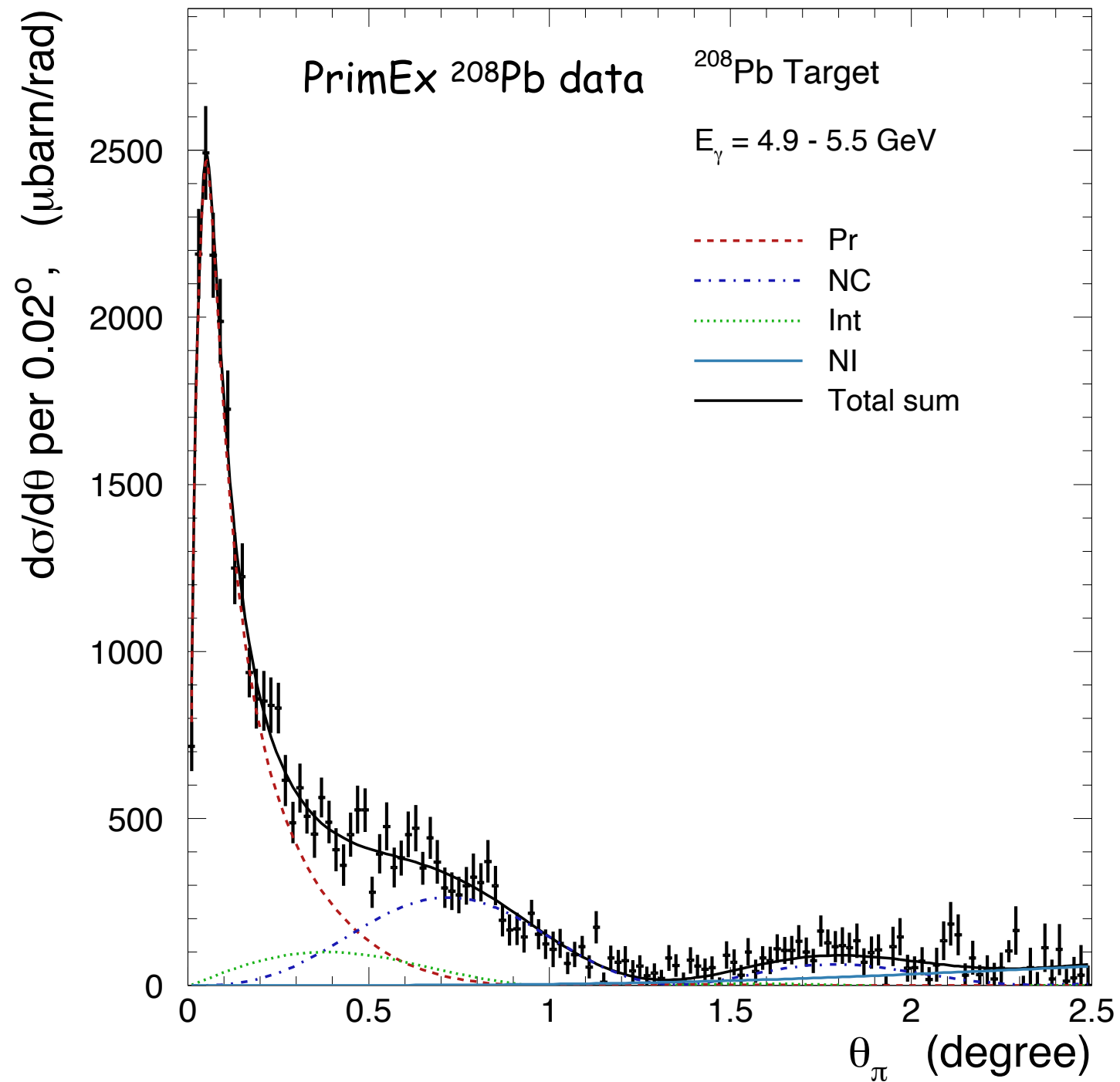


Scaling the Primakoff, coherent and incoherent signals seen in PrimEx to CPP and NPP



Scaling the Primakoff signal seen in PrimEx to NPP

Primakoff production of π^0

$$\frac{d\sigma_{PrimEx}}{d\Omega} = \Gamma_{\gamma\gamma} \frac{8\alpha Z^2}{M_\pi^3} \frac{\beta^3 E^4}{Q^4} F_{EM}^2(Q^2) \sin^2\theta$$

$$\Gamma_{\gamma\gamma} = 7.7 \text{ eV}$$

Primakoff production of $\pi^0\pi^0$

$$\frac{d\sigma_{NPP}}{d\Omega dM_{\pi\pi}} = \frac{2\alpha Z^2}{\pi^2 M_{\pi\pi}} \frac{\beta^2 E^4}{Q^4} F_{EM}^2(Q^2) \sin^2\theta \sigma(\gamma\gamma \rightarrow \pi^0\pi^0)$$

$$\frac{d\sigma_{NPP}}{d\Omega dM_{\pi\pi}} = \left[\frac{1}{4\pi^2} \frac{M_{\pi\pi}^2}{\beta} \sigma(\gamma\gamma \rightarrow \pi^0\pi^0) \right] \frac{8\alpha Z^2}{M_{\pi\pi}^3} \frac{\beta^3 E^4}{Q^4} F_{EM}^2(Q^2) \sin^2\theta$$

$$\frac{d\sigma_{NPP}}{d\Omega} \approx \left[\frac{1}{4\pi^2} \frac{M_{\pi\pi}^2}{\beta} \sigma(\gamma\gamma \rightarrow \pi^0\pi^0) \Delta M_{\pi\pi} \right] \frac{8\alpha Z^2 \beta^3 E^4}{M_{\pi\pi}^3 Q^4} F_{EM}^2(Q^2) \sin^2\theta$$

$$\frac{d\sigma_{NPP}}{d\Omega} \approx \Gamma_{NPP} \frac{8\alpha Z^2 \beta^3 E^4}{M_{\pi\pi}^3 Q^4} F_{EM}^2(Q^2) \sin^2\theta$$

$$\Gamma_{NPP} \equiv \frac{1}{4\pi^2} \frac{M_{\pi\pi}^2}{\beta} \sigma(\gamma\gamma \rightarrow \pi^0\pi^0) \Delta M_{\pi\pi}$$

$$M_{\pi\pi} \approx 0.4 \text{ GeV} \quad \Delta M_{\pi\pi} \approx 0.4 \text{ GeV} \quad \beta = 1 \quad \sigma(\gamma\gamma \rightarrow \pi^0\pi^0) \approx 10 \text{ nb}$$

$$\Gamma_{NPP} = 42 \text{ eV}$$

$$\frac{d\sigma_{NPP}}{d\Omega dM_{\pi\pi}} \Delta M_{\pi\pi} / \frac{d\sigma_{PrimEx}}{d\Omega} \approx 5.5$$

Scaling the coherent signal seen in PrimEx to NPP

$$\frac{d\sigma_{\gamma A \rightarrow A\pi^0\pi^0}}{dt} \approx \eta^2 A^2 \frac{d\sigma_{\gamma N \rightarrow N\pi^0\pi^0}}{dt} F^2(t)$$

η = nuclear absorption factor for one π^0

A = nuclear mass number

$\frac{d\sigma_{\gamma N \rightarrow N\pi^0\pi^0}}{dt}$ = photoproduction cross section on the nucleon

$F^2(t)$ = nuclear form factor

Data for $f_0(500)$

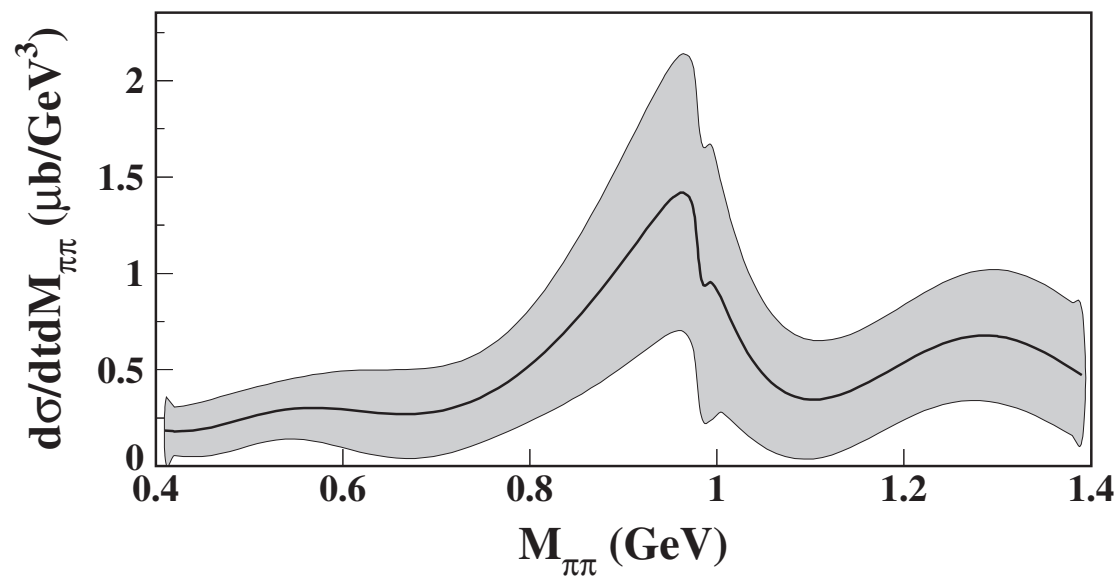
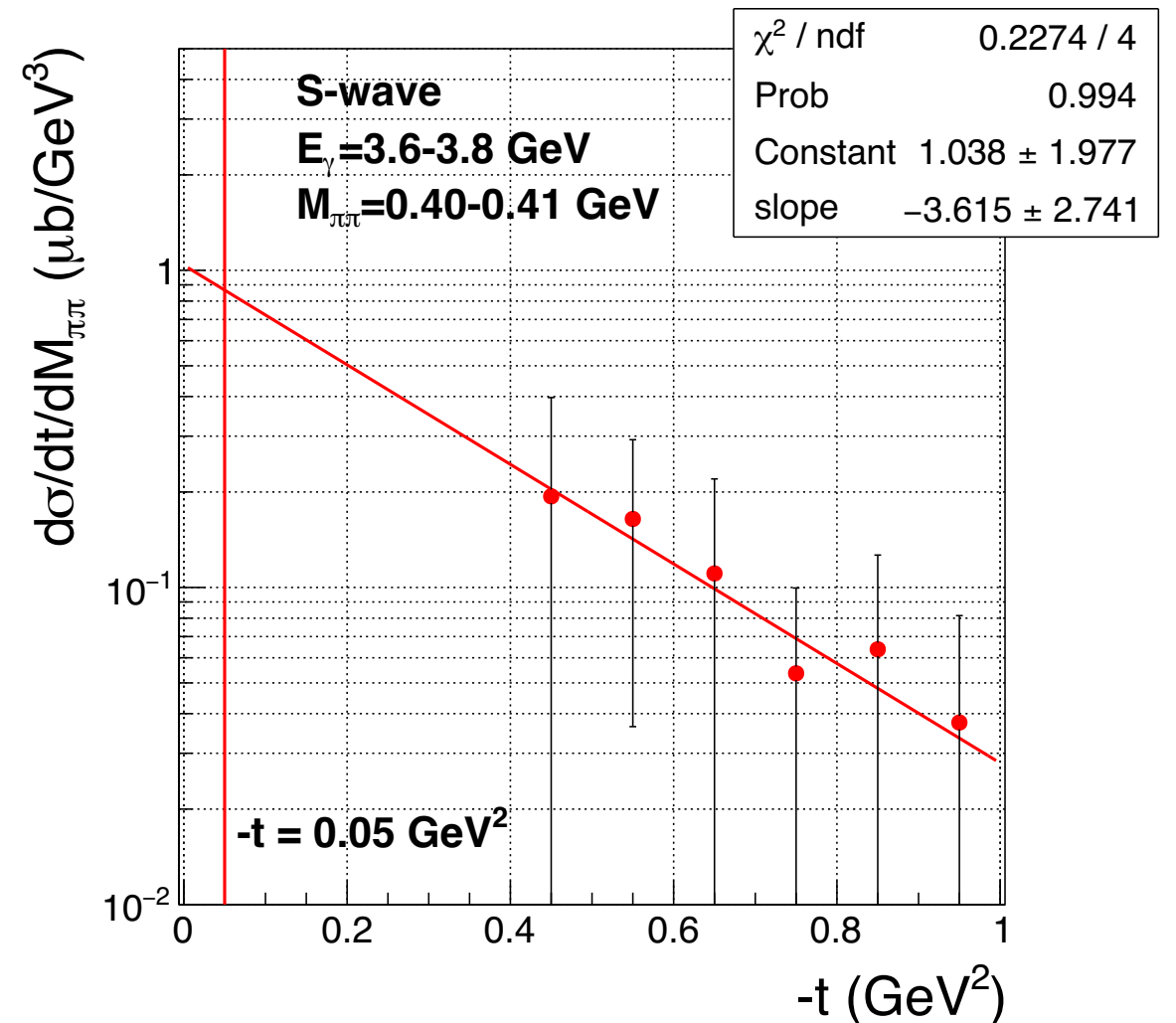


FIG. 12. S -wave cross section derived by the fit in the $3.2 < E_\gamma < 3.4$ GeV and $0.5 < -t < 0.6$ GeV² bin. The systematic and the fit uncertainties are added in quadrature and are shown by the gray band.

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$$\frac{d\sigma_{\gamma N \rightarrow N\pi\pi}}{dt} = 1.0 \frac{\mu b}{\text{GeV}^3} \times 0.4 \text{ GeV} \times \frac{1}{2} = 0.2 \frac{\mu b}{\text{GeV}^2}$$

I expect the cross section to be smaller at 6.0 GeV

Data for π^0 photo-production on the nucleon

$$\frac{d\sigma_{\gamma N \rightarrow N\pi^0}}{dt} = 1.5 \frac{\mu b}{\text{GeV}^2} @ 6 \text{ GeV}$$

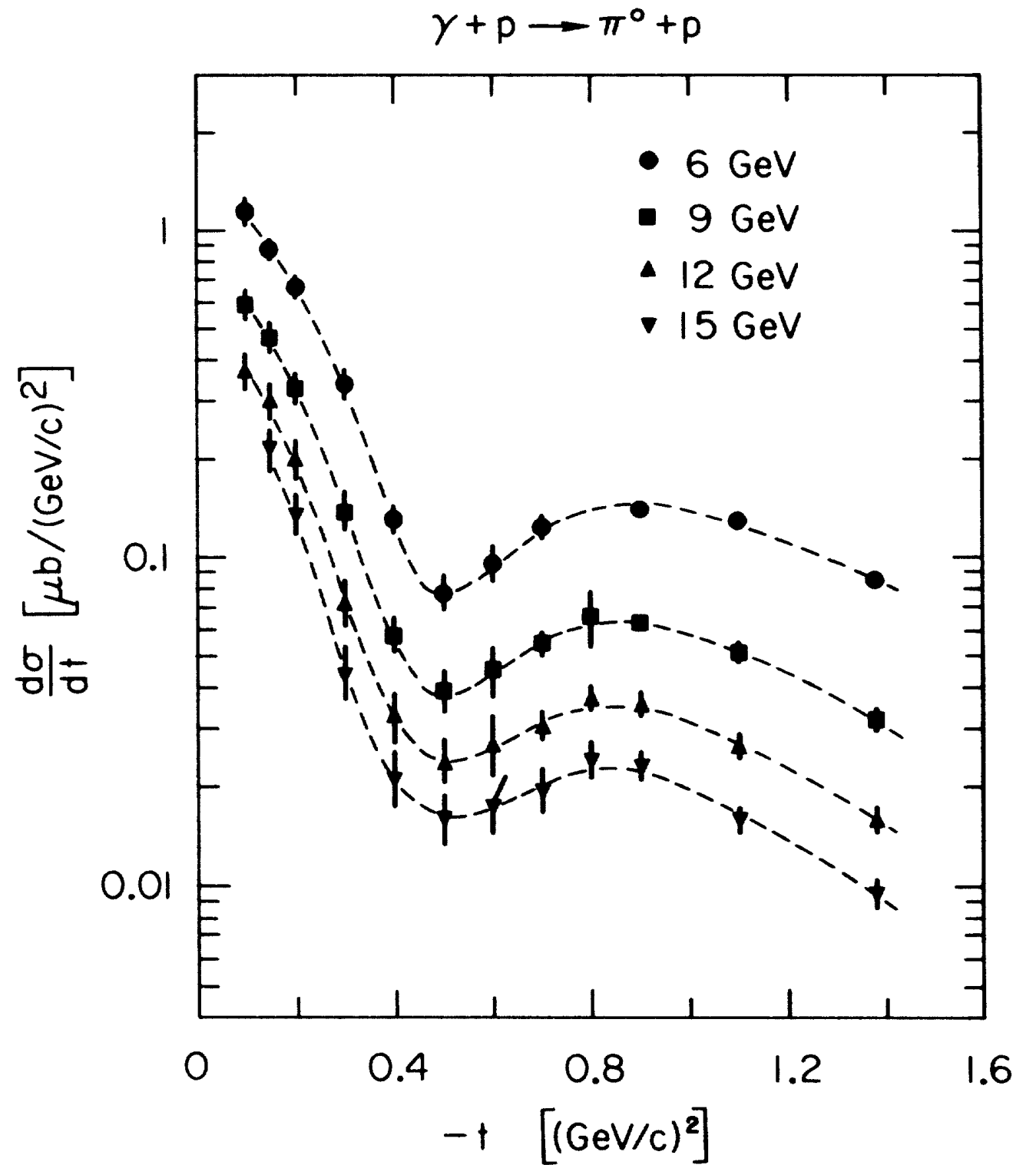


Fig. 5. $d\sigma/dt$ in $\mu b/(\text{GeV}/c)^2$ is plotted versus $|t|$ for incident photon energies of 6, 9, 12, and 15 GeV. The dashed lines are only to guide the eye.

η = nuclear absorption factor for second π^0 = 0.45 (Is this correct ?)

$$\frac{d\sigma_{\gamma N \rightarrow N\pi^0\pi^0}}{dt} / \frac{d\sigma_{\gamma N \rightarrow N\pi^0}}{dt} = \frac{0.2}{1.5} = 0.13$$

Assume $F_{NPP}^2(t) / F_{PrimEx}^2(t) \approx 1$

$$\frac{d\sigma_{\gamma A \rightarrow A\pi^0\pi^0}}{dt} / \frac{d\sigma_{\gamma A \rightarrow A\pi^0}}{dt} \approx 0.06$$

Scaling the incoherent signal seen in PrimEx to NPP

$$\frac{d\sigma_{\gamma A \rightarrow \pi^0 \pi^0}}{dt} \approx \eta^2 A (1 - G(t)) \frac{d\sigma_{\gamma N \rightarrow N \pi^0 \pi^0}}{dt}$$

η = nuclear absorption factor for one π^0 = .45 ?

A = nuclear mass number

$\frac{d\sigma_{\gamma N \rightarrow N \pi^0 \pi^0}}{dt}$ = photoproduction cross section on the nucleon

$1-G(t)$ = Pauli suppression factor, assumed equal for PrimEx and NPP

$$\frac{d\sigma_{\gamma A \rightarrow \pi^0 \pi^0}}{dt} / \frac{d\sigma_{\gamma A \rightarrow \pi^0}}{dt} \approx 0.06$$

Increases by a factor of $\times 5.5$

